

UNCLASSIFIED



Australian Government

Department of Defence

Science and Technology

# Program Analysis for Reverse Engineers

From  $\top$  to  $\perp$

Adrian Herrera

Defence Science and Technology Group

April 25, 2023

## \$ whoami

- Researcher with the Defence Science and Technology (DST) Group
- Visiting researcher at the Australian National University (ANU)
- Interested in applying academic research to reverse engineering problems

## Outline

1. Introduction
2. SMT solvers
3. Symbolic execution
4. Abstract interpretation
5. Conclusion

# Introduction

## What is program analysis?

- Automatically reason about a computer program's behaviour
- Active research field for decades
  - E.g. compilers
- What do we want to reason about?
  - **Security**: Can we overflow this array?
  - **Correctness**: Does this loop terminate?
  - **Compiler optimisations**: Is this code reachable?

## Static vs. dynamic analysis

Two flavours of program analysis

- **Static analysis:** Analyse the program **without** running it
- **Dynamic analysis:** Analyse the program **while** running it

## Static vs. dynamic analysis

Two flavours of program analysis

- **Static analysis:** Analyse the program **without** running it
- **Dynamic analysis:** Analyse the program **while** running it

### Static analysis

- ✓ Reason about **all** executions
- ✗ Less precise

## Static vs. dynamic analysis

Two flavours of program analysis

- **Static analysis:** Analyse the program **without** running it
- **Dynamic analysis:** Analyse the program **while** running it

### Static analysis

- ✓ Reason about **all** executions
- ✗ Less precise

### Dynamic analysis

- ✗ Reason about **observed** executions
- ✓ More precise



## Static vs. dynamic analysis

Two flavours of program analysis

- **Static analysis:** Analyse the program **without** running it
- **Dynamic analysis:** Analyse the program **while** running it

### Static analysis

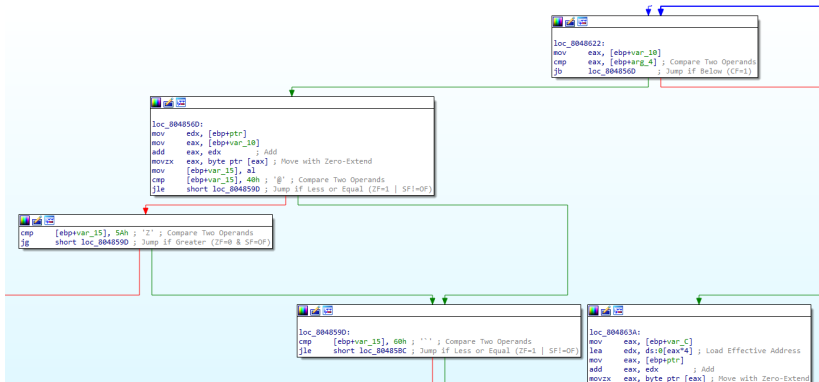
- ✓ Reason about **all** executions
- ✗ Less precise

### Dynamic analysis

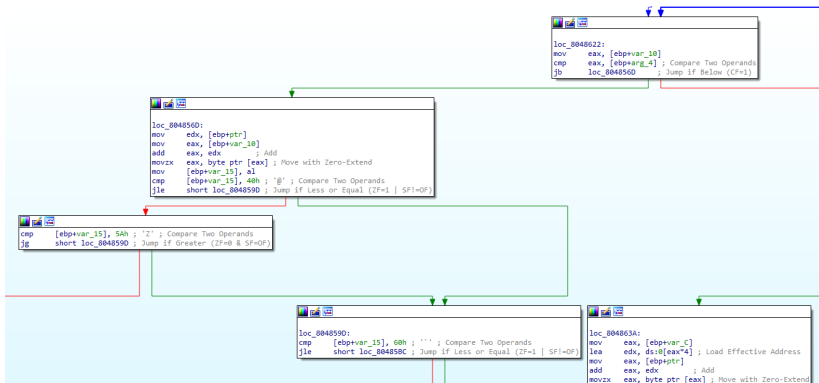
- ✗ Reason about **observed** executions
- ✓ More precise

As a reverse engineer, you already use program analysis

# Static analysis

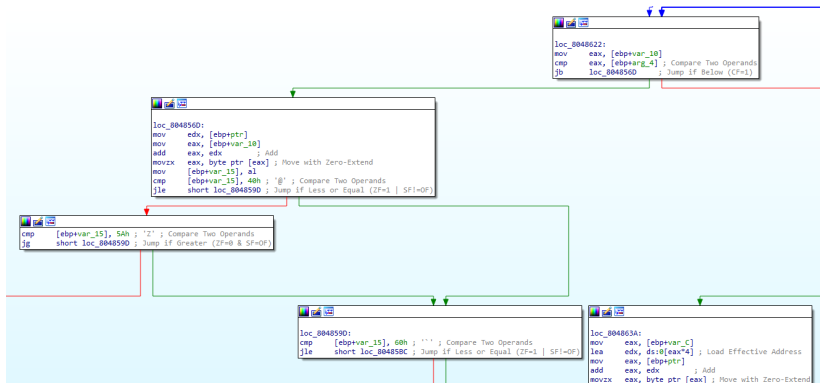


# Static analysis



- Disassembly
- Control-flow graph recovery
- Jump-table recovery

# Static analysis



- Disassembly
- Control-flow graph recovery
- Jump-table recovery

**Program analysis**

# Dynamic analysis

## Input Sample

PID: 3720, Report UID: 00015093-00003720

MD5: c52f20a854efb013a0a1248fd84aaa95

SHA256: cf8533849ee5e82023ad7adbdbd6543cb6db596c53048b1a0c00b3643a72db30

x

API calls **Registry** Mutants Handles Modules Files Streams (1)

NtCreateFile@NTDLL.dll	pFileHandle	0
	DesiredAccess	80100080
	ObjectAttributes	1800000000000000ecc9270040000000000000d8c92700
	IoStatusBlock	185c469400000000
	FileAttributes	0
	ShareAccess	1
	CreateDisposition	1
	CreateOptions	60
	EaBuffer	0
	EaLength	0
	(status)	STATUS_OBJECT_NAME_NOT_FOUND (c0000034)
	(name)	%WINDIR%\assembly\NativeImages_v2.0.50727_32\index23b.dat
NtDelayExecution@NTDLL.dll	Alertable	0
	(originaldelay)	00000030

# Dynamic analysis

## Input Sample

PID: 3720, Report UID: 00015093-00003720

MD5: c52f20a854efb013a0a1248fd84aaa95

SHA256: cf8533849ee5e82023ad7adbdbd6543cb6db59c53048b1a0c00b3643a72db30

x

API calls   Registry   Mutants   Handles   Modules   Files   Streams (1)

NtCreateFile@NTDLL.DLL	pFileHandle	0
	DesiredAccess	80100080
	ObjectAttributes	1800000000000000ecc9270040000000000000d8c92700
	IoStatusBlock	185c469400000000
	FileAttributes	0
	ShareAccess	1
	CreateDisposition	1
	CreateOptions	60
	EaBuffer	0
	EaLength	0
	(status)	STATUS_OBJECT_NAME_NOT_FOUND (c0000034)
	(name)	%WINDIR%\assembly\NativeImages_v2.0.50727_32\index23b.dat
NtDelayExecution@NTDLL.DLL	Alertable	0
	(originaldelay)	00000030

- API monitoring
- Code coverage

# Dynamic analysis

## Input Sample

PID: 3720, Report UID: 00015093-00003720

MD5: c52f20a854efb013a0a1248fd84aaa95

SHA256: cf8533849ee5e82023ad7adbdbd6543cb6db596c53048b1a0c00b3643a72db30

x

API calls   Registry   Mutants   Handles   Modules   Files   Streams (1)

NtCreateFile@NTDLL.dll	pFileHandle	0
	DesiredAccess	80100080
	ObjectAttributes	180000000000000ecc927004000000000000d8c92700
	IoStatusBlock	185c469400000000
	FileAttributes	0
	ShareAccess	1
	CreateDisposition	1
	CreateOptions	60
	EaBuffer	0
	EaLength	0
	(status)	STATUS_OBJECT_NAME_NOT_FOUND (c0000034)
	(name)	%WINDIR%\assembly\NativeImages_v2.0.50727_32\index23b.dat
NtDelayExecution@NTDLL.dll	Alertable	0
	(originaldelay)	00000030

- API monitoring
  - Code coverage
- } **Program analysis**

# Program analysis in academia

## A Galois Connection Calculus for Abstract Interpretation\*

Patrick Cousot

CIMS\*\*, NYU, USA pcousot@cims.nyu.edu

Radhia Cousot

CNRS Emeritus, ENS, France rcousot@ens.fr

**Abstract** We introduce a Galois connection calculus for language independent specification of abstract interpretations used in programming language semantics, formal verification, and static analysis. This Galois connection calculus and its type system are typed by abstract interpretation.

**Categories and Subject Descriptors** D.2.4 [Software/Program Verification]  
**General Terms** Algorithms, Languages, Reliability, Security, Theory, Verification.  
**Keywords** Abstract Interpretation, Galois connection, Static Analysis, Verification.

**1. Galois connections in Abstract Interpretation** In *Abstract interpretation* [3, 4, 6, 7] concrete properties (for example (e.g.) of computations) are related to abstract properties (e.g. types). The abstract properties are always *sound* approximations of the concrete properties (abstract proofs/static analyzes are always correct in the concrete) and are sometimes *complete* (proofs/analyzes of abstract properties can all be done in the abstract only). E.g. types are sound but incomplete [2] while abstract semantics are usually complete [9]. The *concrete domain*  $(C, \sqsubseteq)$  and *abstract domain*  $(A, \preceq)$  of properties are posets (partial orders being interpreted as implication). When concrete properties all have a  $\preceq$ -most precise abstraction, the correspondence is a *Galois connection* (GC)  $(C, \sqsubseteq) \xrightarrow{\gamma} (A, \preceq)$  with *abstraction*  $\alpha \in C \mapsto A$  and *concretization*  $\gamma \in A \mapsto C$  satisfying  $\forall P \in C : \forall Q \in A : \alpha(Q) \preceq y \Leftrightarrow x \sqsubseteq \gamma(y) \Leftrightarrow$  expresses soundness and  $\Leftarrow$  best abstraction). Each adjoint  $\alpha/\gamma$  uniquely determines the other  $\gamma/\alpha$ . A *Galois retraction* (or *insertion*) has  $\alpha$  onto, so  $\gamma$  is one-to-one, and  $\alpha \circ \gamma$  is the identity. E.g. the *interval abstraction*  $S[\cdot]$  [3, 4] of the power set  $\wp(C)$  of complete  $\leq$ -totally ordered sets  $C \cup \{-\infty, \infty\}$  is  $S[\cdot] : (C, \leq) \rightarrow (-\infty, \infty]$   $\hat{=} (\wp(C), \sqsubseteq) \xrightarrow{\gamma} (I(C \cup \{-\infty, \infty\}), \leq)$  with  $\alpha^x(X) \hat{=} [\min X, \max X]$ ,  $\min \emptyset \hat{=} \infty$ ,  $\max \emptyset \hat{=} -\infty$ ,  $\gamma^y([a, b]) \hat{=} \{x \in C \mid a \leq x \leq b\}$ , intervals  $S[\cdot] : (C \cup \{-\infty, \infty\}, \leq) \hat{=} \{\{a, b\} \mid a \in C \cup \{-\infty\} \wedge b \in C \cup \{\infty\} \wedge a \leq b\} \cup \{\{\infty, -\infty\}\}$ , and inclusion  $[a, b] \sqsubseteq [c, d] \hat{=} c \leq a \wedge b \leq d$ . A *Galois isomorphism*  $(C, \sqsubseteq) \xrightarrow{\gamma} (A, \preceq)$  has both  $\alpha$  and  $\gamma$  bijective. E.g. global and local invariants are isomorphic by the *right image abstraction*  $S[\cdot] : (\mathcal{L}, \mathcal{M}) \hat{=} (\wp(\mathcal{L} \times \mathcal{M}), \sqsubseteq) \xrightarrow{\gamma} (\mathcal{L}, \preceq)$  with  $\alpha^r(P) \hat{=} \lambda \ell \cdot \{m \mid (\ell, m) \in P\}$ ,  $\gamma^r(Q) \hat{=} \{\{\ell, m\} \mid m \in Q(\ell)\}$ , and  $\sqsubseteq$  is the pointwise extension of inclusion  $\subseteq$ .

**3. Basic GC semantics** Basic GCs are primitive abstractions of properties. Classical examples are the *identity abstraction*  $S[\cdot] : (C, \sqsubseteq) \hat{=} (C, \sqsubseteq) \xrightarrow{\lambda Q \cdot Q} (C, \sqsubseteq)$ , the *top abstraction*  $S[\cdot] : (C, \sqsubseteq) \hat{=} (C, \sqsubseteq) \xrightarrow{\lambda P \cdot P} (C, \sqsubseteq)$ , the *join abstraction*  $S[\cdot] : (C, \sqsubseteq) \hat{=} (C, \sqcup) \xrightarrow{\lambda Q \cdot \top} (C, \sqcup)$ , the *meet abstraction*  $S[\cdot] : (C, \sqsubseteq) \hat{=} (C, \sqcap) \xrightarrow{\lambda Q \cdot \perp} (C, \sqcap)$ , the *complement abstraction*  $S[\cdot] : (C, \sqsubseteq) \hat{=} (\wp(C), \sqsubseteq) \xrightarrow{\lambda Q \cdot \neg Q} (\wp(C), \sqsubseteq)$ , the *finite/infinite sequence abstraction*  $S[\cdot] : \omega(C) \hat{=} (\wp(C^\infty), \sqsubseteq) \xrightarrow{\lambda Q \cdot Q^\infty} (\wp(C), \sqsubseteq)$  with  $\alpha^\omega(P) \hat{=} \{\sigma \mid \sigma \in P \wedge i \in \text{dom}(\sigma)\}$  and  $\gamma^\omega(Q) \hat{=} \{\sigma \in C^\infty \mid \forall i \in \text{dom}(\sigma) : \sigma_i \in Q\}$ , the *transformer abstraction*  $S[\cdot] : (C_1, C_2) \hat{=} (\wp(C_1 \times C_2), \sqsubseteq) \xrightarrow{\lambda Q \cdot Q^{-1}} (\wp(C_1), \sqsubseteq) \xrightarrow{\lambda Q \cdot Q} (\wp(C_2), \sqsubseteq)$  mapping relations to join-preserving transformers with  $\alpha^-(R) \hat{=} \lambda X \cdot \{y \mid \exists x \in X : (x, y) \in R\}$ ,  $\gamma^-(g) \hat{=} \{(x, y) \mid y \in g(\{x\})\}$ , the *function abstraction*  $S[\cdot] : (C_1, C_2) \hat{=} (\wp(C_1 \mapsto C_2), \sqsubseteq) \xrightarrow{\lambda Q \cdot Q} (\wp(C_1), \mapsto \wp(C_2), \sqsubseteq)$  with  $\alpha^-(P) \hat{=} \lambda X \cdot \{f(x) \mid f \in P \wedge x \in X\}$ ,  $\gamma^-(g) \hat{=} \{f \in C_1 \mapsto C_2 \mid \forall X \in \wp(C_1) : \forall x \in X : f(x) \in g(X)\}$ , the *cartesian abstraction*  $S[\cdot] : (I, C) \hat{=} (\wp(I \mapsto C), \sqsubseteq) \xrightarrow{\lambda Q \cdot Q} (I \mapsto \wp(C), \sqsubseteq)$  with  $\alpha^x(X) \hat{=} \lambda i \in I \cdot \{x \in C \mid \exists f \in I \mapsto C : f[i \mapsto x] \in X\}$ ,  $\gamma^x(Y) \hat{=} \{f \mid \forall i \in I : f(i) \in Y(i)\}$ , and the pointwise extension  $\sqsubseteq$  of  $\subseteq$  to  $I, \text{etc}$ .

**4. Galois connector semantics** *Galois connectors* build a GC from GCs provided as parameters. Unary Galois connectors include the *reduction connector*  $S[\cdot] : (C, \sqsubseteq) \xrightarrow{\gamma} (A, \preceq) \hat{=} (C, \sqsubseteq) \xrightarrow{\gamma} (\{\{\alpha(P) \mid P \in C\}, \preceq\})$  and the *pointwise connector*  $S[\cdot] : (C, \sqsubseteq) \xrightarrow{\gamma} (C, \preceq) \hat{=} (X \mapsto C, \sqsubseteq) \xrightarrow{\lambda P \cdot \alpha P} (X \mapsto A, \preceq)$  for the pointwise orderings  $\sqsubseteq$  and  $\preceq$ . Binary Galois connectors include the *composition connector*  $S[\cdot] : (C, \sqsubseteq) \xrightarrow{\gamma_1} (A_1, \preceq) \hat{=} (A_2, \preceq) \xrightarrow{\gamma_2} (A_3, \preceq) \hat{=} [(A_1, \preceq) \circ (A_2, \preceq)] \hat{=} (C, \sqsubseteq) \xrightarrow{\gamma_1 \circ \gamma_2} (A_3, \preceq) \hat{=} \Omega$  (where  $\Omega$  is a static error), the *prod-*



# Program analysis in academia

## A Galois Connection Calculus for Abstract Interpretation\*

Patrick Cousot<sup>1</sup> and Radhia Cousot<sup>2</sup>

<sup>1</sup>CIMS\*\*, NYU, USA [pcousot@nyu.edu](mailto:pcousot@nyu.edu) <sup>2</sup>CNRS, ENSI, France [cousot@ens.fr](mailto:cousot@ens.fr)

**Abstract** We introduce a Galois connection calculus for language independent specification of abstract interpretation. The calculus is based on programming language semantics, formal verification, and static analysis. The calculus is a Galois connection calculus and its type system are typed by abstract interpretation.

**Categories and Subject Descriptors** D.3.2 [Software/Program Verification] Algorithms, Languages, Reliability, Security, Theory, Verification.  
**Keywords** Abstract Interpretation, Galois connection, Static Analysis, Verification.

**1. Galois connection for Abstract Interpretation** In *Abstract interpretation* [3, 4] concrete properties (for example (e.g.) of computations) are related to abstract properties (e.g. types). The abstract properties are always *sound* approximations of the concrete properties. Abstract proofs/static analyzes are always correct in the concrete. Abstract proofs/static analyzes are sometimes *complete* (proofs/analyzes of abstract properties can all be done in the abstract only). E.g. types are sound but not complete [2] while abstract semantics are usually complete [9]. A *concrete domain*  $(C, \sqsubseteq)$  and *abstract domain*  $(A, \preceq)$  are posets (partial orders being interpreted as implication). Concrete properties all have a  $\preceq$ -most precise abstraction. This correspondence is a *Galois connection* (GC)  $(\alpha, \gamma)$   $(\sqsubseteq, \preceq)$  with *abstraction*  $\alpha \in C \mapsto A$  and *concretization*  $\gamma \in A \mapsto C$  satisfying  $\forall P \in C : \forall Q \in A : \alpha(P) \preceq Q \Leftrightarrow P \sqsubseteq \gamma(Q)$  (which ensures soundness and  $\Leftarrow$  best abstraction). Each adjoint  $\alpha/\gamma$  uniquely determines the other  $\gamma/\alpha$ . A *retraction* (or *injection*) is an onto, so  $\gamma$  is one-to-one and  $\alpha$  is the identity. E.g. the *pointwise abstraction* [3, 4]  $\alpha^x(C) \in A$  over set  $\wp(C)$  of complete  $\leq$ -totally ordered sets  $C \cup \{\perp, \infty\}$  is  $S[\llbracket(C, \leq), (-\infty, \infty)\rrbracket] \triangleq (\wp(C), \subseteq)$  with  $\alpha^x(C) \triangleq \{a \in A \mid \exists c \in C : c \leq a\}$  and  $\gamma^x(a) \triangleq \max \emptyset \triangleq -\infty, \gamma^x([a, b]) \triangleq \{x \in C \mid a \leq x \leq b\}$ . The *pointwise concretization*  $\gamma^x(C) \triangleq \{[a, b] \mid a \in C \cup \{-\infty\}, b \in C \cup \{\infty, -\infty\}\}$ , and inclusion  $[a, b] \in [c, d] \Leftrightarrow a \leq c \wedge b \leq d$ . A *Galois isomorphism*  $(C, \sqsubseteq) \xrightarrow{\alpha, \gamma} (A, \preceq)$  has  $\alpha, \gamma$  bijective. E.g. global and local invariants are isomorphic by *pointwise abstraction*  $S[\llbracket\mathcal{L}, \mathcal{M}\rrbracket] \triangleq (\wp(\mathcal{L} \times \mathcal{M}), \subseteq)$  with  $\alpha^x(P) \triangleq \{(\ell, m) \in \mathcal{L} \times \mathcal{M} \mid \ell \in P\}$  and  $\gamma^x(Q) \triangleq \{(\ell, m) \in \mathcal{L} \times \mathcal{M} \mid \ell \in Q \wedge m \in Q\}$ , and  $\subseteq$  is the pointwise extension of inclusion  $\subseteq$ .

**3. Basic GC semantics** GCs are primitive abstractions of properties. Classical examples are *identity abstraction*  $S[\llbracket(C, \sqsubseteq)\rrbracket] \triangleq (C, \sqsubseteq) \xrightarrow{\lambda Q \cdot Q} (C, \sqsubseteq)$  and *top abstraction*  $S[\llbracket\top(C, \sqsubseteq)\rrbracket] \triangleq (C, \sqsubseteq) \xrightarrow{\lambda Q \cdot \top} (\top, \sqsubseteq)$ . *Bottom abstraction*  $S[\llbracket\perp(C, \sqsubseteq)\rrbracket] \triangleq (C, \sqsubseteq) \xrightarrow{\lambda Q \cdot \perp} (\perp, \sqsubseteq)$  with  $\perp \triangleq \perp P, \gamma^x(Q) \triangleq \langle \wp(C), \subseteq \rangle$ . *Compositional abstraction*  $S[\llbracket(C, \sqsubseteq) \times (C, \sqsubseteq)\rrbracket] \triangleq (\langle \wp(C), \subseteq \rangle, \subseteq) \xrightarrow{\lambda X \cdot X} (\langle \wp(C), \subseteq \rangle, \subseteq)$ . *Finite sequence abstraction*  $S[\llbracket\infty(C)\rrbracket] \triangleq (\langle \wp(C^\infty), \subseteq \rangle, \subseteq)$  with  $\alpha^x(P) \triangleq \{\sigma \in P \mid \sigma \in P \wedge i \in \text{dom}(\sigma) \Rightarrow \gamma^x(Q) \triangleq \{\sigma \in C^\infty \mid \forall i \in \text{dom}(\sigma) : \sigma_i \in Q\}$ , the *pointwise abstraction*  $S[\llbracket\langle C_1, C_2 \rangle\rrbracket] \triangleq (\langle \wp(C_1), \subseteq \rangle, \subseteq) \xrightarrow{\lambda X \cdot X} (\langle \wp(C_2), \subseteq \rangle, \subseteq)$  with  $\alpha^x(R) \triangleq \lambda X \cdot \{y \mid \exists x \in R : \gamma^x(y) \triangleq \{(x, y) \mid y \in g(\{x\})\}$ , the *functorial abstraction*  $S[\llbracket\langle C_1, C_2 \rangle\rrbracket] \triangleq (\langle \wp(C_1 \mapsto C_2), \subseteq \rangle, \subseteq) \xrightarrow{\lambda X \cdot X} (\langle \wp(C_2), \subseteq \rangle, \subseteq)$  with  $\alpha^x(P) \triangleq \lambda X \cdot \{f \in P \mid \forall x \in C_1 : f(x) \in g(X)\}$ ,  $\gamma^x(g) \triangleq \{f \in C_1 \mapsto C_2 \mid \forall X \in \wp(C_1) : \forall x \in X : f(x) \in g(X)\}$ , the *cartesian abstraction*  $S[\llbracket I, C \rrbracket] \triangleq (\langle \wp(I \times C), \subseteq \rangle, \subseteq) \xrightarrow{\lambda X \cdot X} (\langle \wp(C), \subseteq \rangle, \subseteq)$  with  $\alpha^x(X) \triangleq \lambda i \in I \cdot \{c \in C \mid \exists f \in I \mapsto C : f[i \mapsto x] \in X\}$ ,  $\gamma^x(Y) \triangleq \{f \mid \forall i \in I : f(i) \in Y(i)\}$ , and the *pointwise extension*  $\subseteq$  of  $\subseteq$  to  $I$ , etc.

**4. Galois connector semantics** *Connectors* build a GC from GCs provided as parameters. Galois connectors include the *reduction connector*  $S[\llbracket(A, \preceq)\rrbracket] \triangleq (C, \sqsubseteq) \xrightarrow{\gamma} (A, \preceq)$  and the *pointwise connector*  $S[X \mapsto (C, \sqsubseteq) \times (A, \preceq)] \triangleq (X \mapsto C, \sqsubseteq) \xrightarrow{\lambda P \cdot \alpha \circ P} (X \mapsto A, \preceq)$  with  $\alpha^x(X) \triangleq \{x \in X \mid \exists c \in C : c \in x\}$  and  $\gamma^x(Y) \triangleq \{c \in C \mid \exists f \in Y : f(c) \in Y\}$ . Binary Galois connectors include the *composition connector*  $S[\llbracket(C, \sqsubseteq) \times (C, \sqsubseteq)\rrbracket] \triangleq (C, \sqsubseteq) \xrightarrow{\gamma_2} (C, \sqsubseteq) \xrightarrow{\gamma_1} (C, \sqsubseteq)$  (where  $\Omega$  is a static error), the *prod-*

## Aims

- ✓ Introduce new program analysis techniques
- ✓ Focus on reverse engineering
- ✓ Example based

## Aims

- ✓ Introduce new program analysis techniques
- ✓ Focus on reverse engineering
- ✓ Example based
- ✗ Limit the maths
- ✗ Limit the code

## Aims

- ✓ Introduce new program analysis techniques
- ✓ Focus on reverse engineering
- ✓ Example based
- ✗ Limit the maths
- ✗ Limit the code
- ✗ Won't focus on specific ISA
- ✓ Perform analysis on an IR

## Aims

- ✓ Introduce new program analysis techniques
- ✓ Focus on reverse engineering
- ✓ Example based
- ✗ Limit the maths
- ✗ Limit the code
- ✗ Won't focus on specific ISA
- ✓ Perform analysis on an IR
  - REIL

## Reverse Engineering Intermediate Language (REIL)

- Developed by Zynamics (now Google)
- Used in Binnavi
- Simple, reduced instruction set
  - No implicit side effects
  - 17 instructions
  - All instructions take 3 operands (may be unused)

## REIL syntax & semantics

```
0001: xor [DWORD r1, DWORD r1, DWORD r1]
0002: add [DWORD 10, DWORD r1, DWORD r1]
0003: str [DWORD 20, , DWORD r2]
0004: add [DWORD r1, DWORD r2, DWORD r1]
0005: stm [DWORD r1, , DWORD 0x12345678]
```

## REIL syntax & semantics

```
0001: xor [DWORD r1, DWORD r1, DWORD r1]
0002: add [DWORD 10, DWORD r1, DWORD r1]
0003: str [DWORD 20, , DWORD r2]
0004: add [DWORD r1, DWORD r2, DWORD r1]
0005: stm [DWORD r1, , DWORD 0x12345678]
```

Important to differentiate between **syntax** and **semantics**



## REIL syntax & semantics

```
0001: xor [DWORD r1, DWORD r1, DWORD r1]
0002: add [DWORD 10, DWORD r1, DWORD r1]
0003: str [DWORD 20, , DWORD r2]
0004: add [DWORD r1, DWORD r2, DWORD r1]
0005: stm [DWORD r1, , DWORD 0x12345678]
```

Important to differentiate between **syntax** and **semantics**

**Syntax**      The words (*symbols*) that make up a sentence

**Semantics**    The *meaning* behind the sentence

## REIL syntax & semantics

```
0001: xor [DWORD r1, DWORD r1, DWORD r1]
0002: add [DWORD 10, DWORD r1, DWORD r1]
0003: str [DWORD 20, , DWORD r2]
0004: add [DWORD r1, DWORD r2, DWORD r1]
0005: stm [DWORD r1, , DWORD 0x12345678]
```

Important to differentiate between **syntax** and **semantics**

### Syntax

Instructions	xor, add, str, ...
Operand sizes	BYTE, WORD, DWORD, ...
Registers	r1, r2, ...
Literals	10, 0x12345678, ...

## REIL syntax & semantics

```
0001: xor [DWORD r1, DWORD r1, DWORD r1]
0002: add [DWORD 10, DWORD r1, DWORD r1]
0003: str [DWORD 20, , DWORD r2]
0004: add [DWORD r1, DWORD r2, DWORD r1]
0005: stm [DWORD r1, , DWORD 0x12345678]
```

Important to differentiate between **syntax** and **semantics**

### Semantics

`add [DWORD 10, DWORD r1, DWORD r1]`

1. Look up the value of register r1
2. Add the value 10 to the value from 1.
3. Store the result of 2. in register r1

**Let's do some program analysis!**

# SMT solvers

## Modelling code with maths

```
if ((x >= 3 && (y * 2 - x < 20) && !(y > 1 || y >= 10)) &&  
    (x * y * z == -50)) {  
    // ...  
}
```

## Modelling code with maths

```
if ((x >= 3 && (y * 2 - x < 20) && !(y > 1 || y >= 10)) &&  
    (x * y * z == -50)) {  
    // ...  
}
```

Model this code with a **first-order logic** formula

$$(x \geq 3 \wedge (y \times 2 - x < 20) \wedge \neg (y > 1 \vee y \geq 10)) \wedge (x \times y \times z = -50)$$

## Modelling code with maths

```

if ((x >= 3 && (y * 2 - x < 20) && !(y > 1 || y >= 10)) &&
    (x * y * z == -50)) {
    // ...
}

```

Model this code with a **first-order logic** formula

$$(x \geq 3 \wedge (y \times 2 - x < 20) \wedge \neg (y > 1 \vee y \geq 10)) \wedge (x \times y \times z = -50)$$

conjunction (“and”)

15

negation (“not”)

disjunction (“or”)

DST

Science and Technology for Safeguarding Australia



## Modelling code with maths

We can

## Modelling code with maths

We can

- **Assign** values to the formula's variables ( $x$ ,  $y$  and  $z$ )

## Modelling code with maths

We can

- **Assign** values to the formula's variables ( $x$ ,  $y$  and  $z$ )
- Check if the formula is **satisfiable**

## Modelling code with maths

We can

- **Assign** values to the formula's variables ( $x$ ,  $y$  and  $z$ )
- Check if the formula is **satisfiable**
  - There exists a set of assignments that makes the formula true

## Modelling code with maths

We can

- **Assign** values to the formula's variables ( $x$ ,  $y$  and  $z$ )
- Check if the formula is **satisfiable**
  - There exists a set of assignments that makes the formula true
- Check if the formula is **valid**

## Modelling code with maths

We can

- **Assign** values to the formula's variables ( $x$ ,  $y$  and  $z$ )
- Check if the formula is **satisfiable**
  - There exists a set of assignments that makes the formula true
- Check if the formula is **valid**
  - The formula is true under **all** assignments

## A simple example

$$(x \geq 3 \wedge (y \times 2 - x < 20) \wedge \neg(y > 1 \vee y \geq 10)) \wedge (x \times y \times z = -50)$$

### Assignment

$$x = 5, y = 5, z = -2$$

## A simple example

$$(x \geq 3 \wedge (y \times 2 - x < 20) \wedge \neg(y > 1 \vee y \geq 10)) \wedge (x \times y \times z = -50)$$

### Assignment

$$x = 5, y = 5, z = -2$$

$$(5 \geq 3 \wedge (5 \times 2 - 5 < 20) \wedge \neg(5 > 1 \vee 5 \geq 10)) \wedge (5 \times 5 \times -2 = -50)$$



## A simple example

$$(x \geq 3 \wedge (y \times 2 - x < 20) \wedge \neg(y > 1 \vee y \geq 10)) \wedge (x \times y \times z = -50)$$

### Assignment

$$x = 5, y = 5, z = -2$$

$$(T \wedge (5 < 20) \wedge \neg(T \vee \perp)) \wedge (-50 = -50)$$

## A simple example

$$(x \geq 3 \wedge (y \times 2 - x < 20) \wedge \neg(y > 1 \vee y \geq 10)) \wedge (x \times y \times z = -50)$$

### Assignment

$$x = 5, y = 5, z = -2$$

$$( \uparrow \text{top ("true")} \quad \text{T} \wedge (5 < 20) \wedge \neg(\text{T} \vee \perp) \quad \uparrow \text{bottom ("false")} ) \wedge (-50 = -50)$$

## A simple example

$$(x \geq 3 \wedge (y \times 2 - x < 20) \wedge \neg(y > 1 \vee y \geq 10)) \wedge (x \times y \times z = -50)$$

### Assignment

$$x = 5, y = 5, z = -2$$

$$(T \wedge T \wedge \neg T) \wedge T$$

## A simple example

$$(x \geq 3 \wedge (y \times 2 - x < 20) \wedge \neg(y > 1 \vee y \geq 10)) \wedge (x \times y \times z = -50)$$

### Assignment

$$x = 5, y = 5, z = -2$$

$$(T \wedge T \wedge \perp) \wedge T$$

## A simple example

$$(x \geq 3 \wedge (y \times 2 - x < 20) \wedge \neg(y > 1 \vee y \geq 10)) \wedge (x \times y \times z = -50)$$

### Assignment

$$x = 5, y = 5, z = -2$$

$$\perp \wedge \top$$

## A simple example

$$(x \geq 3 \wedge (y \times 2 - x < 20) \wedge \neg(y > 1 \vee y \geq 10)) \wedge (x \times y \times z = -50)$$

### Assignment

$$x = 5, y = 5, z = -2$$

⊥

## A simple example

$$(x \geq 3 \wedge (y \times 2 - x < 20) \wedge \neg(y > 1 \vee y \geq 10)) \wedge (x \times y \times z = -50)$$

Is the formula valid?

## A simple example

$$(x \geq 3 \wedge (y \times 2 - x < 20) \wedge \neg(y > 1 \vee y \geq 10)) \wedge (x \times y \times z = -50)$$

Is the formula valid? **No**



## A simple example

$$(x \geq 3 \wedge (y \times 2 - x < 20) \wedge \neg(y > 1 \vee y \geq 10)) \wedge (x \times y \times z = -50)$$

Is the formula satisfiable?

## A simple example

$$(x \geq 3 \wedge (y \times 2 - x < 20) \wedge \neg(y > 1 \vee y \geq 10)) \wedge (x \times y \times z = -50)$$

Is the formula satisfiable? **Yes**

## A simple example

$$(x \geq 3 \wedge (y \times 2 - x < 20) \wedge \neg(y > 1 \vee y \geq 10)) \wedge (x \times y \times z = -50)$$

Is the formula satisfiable? **Yes**

When

$$x = 5$$

$$y = -2$$

$$z = 5$$

## General approach

Automate process with a **Satisfiability Modulo Theories (SMT)** solver

## General approach

Automate process with a **Satisfiability Modulo Theories (SMT)** solver

1. Convert code to **static single assignment (SSA)** form

## General approach

Automate process with a **Satisfiability Modulo Theories (SMT)** solver

1. Convert code to **static single assignment (SSA)** form
  - Each variable is assigned exactly once

## General approach

Automate process with a **Satisfiability Modulo Theories (SMT)** solver

1. Convert code to **static single assignment (SSA)** form
  - Each variable is assigned exactly once
  - Reassignments create a new version of that variable

## General approach

Automate process with a **Satisfiability Modulo Theories (SMT)** solver

1. Convert code to **static single assignment (SSA)** form
  - Each variable is assigned exactly once
  - Reassignments create a new version of that variable
2. Model each SSA instruction as a logical formula



## General approach

Automate process with a **Satisfiability Modulo Theories (SMT)** solver

1. Convert code to **static single assignment (SSA)** form
  - Each variable is assigned exactly once
  - Reassignments create a new version of that variable
2. Model each SSA instruction as a logical formula
3. Take the conjunction of all instructions from 2.

## General approach

Automate process with a **Satisfiability Modulo Theories (SMT)** solver

1. Convert code to **static single assignment (SSA)** form
  - Each variable is assigned exactly once
  - Reassignments create a new version of that variable
2. Model each SSA instruction as a logical formula
3. Take the conjunction of all instructions from 2.
4. Query the resulting formula in an SMT solver

## A more complex example

```
0001: xor [r1, r1, r1]
0002: str [-1, , r2]
0003: str [234, , r3]
0004: mul [r2, r3, r3]
0005: xor [r4, r4, r4]
0006: add [r4, r3, r4]
0007: bsh [r4, 1, r5]
0008: add [in, r1, r1]
0009: sub [in, r3, in]
000a: bsh [in, 1, in]
000b: div [r5, 16, r4]
000c: mul [r3, 2, r3]
000d: add [in, r3, r3]
000e: mul [r3, r3, r5]
000f: add [r2, 5, r2]
0010: div [r5, r2, r5]
0011: add [r5, r1, r1]
0012: mod [r1, 2, r3]
0013: jcc [r3, , 0020]
```

0014: ; ...

0020: ; ...

## A more complex example

```

0001: xor [r1, r1, r1_a]
0002: str [-1, , r2]
0003: str [234, , r3]
0004: mul [r2, r3, r3_a]
0005: xor [r4, r4, r4_a]
0006: add [r4_a, r3_a, r4_b]
0007: bsh [r4_b, 1, r5]
0008: add [in, r1_a, r1_b]
0009: sub [in, r3_a, in_a]
000a: bsh [in_a, 1, in_b]
000b: div [r5, 16, r4_c]
000c: mul [r3_a, 2, r3_b]
000d: add [in_b, r3_b, r3_c]
000e: mul [r3_c, r3_c, r5_a]
000f: add [r2, 5, r2_a]
0010: div [r5_a, r2_a, r5_b]
0011: add [r5_b, r1_b, r1_c]
0012: mod [r1_c, 2, r3_d]
0013: jcc [r3_d, , 0020]
  
```

### Convert to SSA

Append `_a`, `_b`, `_c`, etc. to denote reassignments

0014: ; ...

0020: ; ...

## A more complex example

```

0001: xor [r1, r1, r1_a]
0002: str [-1, , r2]
0003: str [234, , r3]
0004: mul [r2, r3, r3_a]
0005: xor [r4, r4, r4_a]
0006: add [r4_a, r3_a, r4_b]
0007: bsh [r4_b, 1, r5]
0008: add [in, r1_a, r1_b]
0009: sub [in, r3_a, in_a]
000a: bsh [in_a, 1, in_b]
000b: div [r5, 16, r4_c]
000c: mul [r3_a, 2, r3_b]
000d: add [in_b, r3_b, r3_c]
000e: mul [r3_c, r3_c, r5_a]
000f: add [r2, 5, r2_a]
0010: div [r5_a, r2_a, r5_b]
0011: add [r5_b, r1_b, r1_c]
0012: mod [r1_c, 2, r3_d]
0013: jcc [r3_d, , 0020]
  
```

### Model as logical formulas

To reach 0014

$$r1_a = r1 \oplus r1$$

$$r2 = -1$$

$$r3 = 234$$

$$r3_a = r2 \times r3$$

$$r4_a = r4 \oplus r4$$

$$r4_b = r4_a + r3_a$$

...

$$r3_d = 0$$

0014: ; ...

0020: ; ...

## A more complex example

```

0001: xor [r1, r1, r1_a]
0002: str [-1, , r2]
0003: str [234, , r3]
0004: mul [r2, r3, r3_a]
0005: xor [r4, r4, r4_a]
0006: add [r4_a, r3_a, r4_b]
0007: bsh [r4_b, 1, r5]
0008: add [in, r1_a, r1_b]
0009: sub [in, r3_a, in_a]
000a: bsh [in_a, 1, in_b]
000b: div [r5, 16, r4_c]
000c: mul [r3_a, 2, r3_b]
000d: add [in_b, r3_b, r3_c]
000e: mul [r3_c, r3_c, r5_a]
000f: add [r2, 5, r2_a]
0010: div [r5_a, r2_a, r5_b]
0011: add [r5_b, r1_b, r1_c]
0012: mod [r1_c, 2, r3_d]
0013: jcc [r3_d, , 0020]
  
```

### Model as logical formulas

To reach 0020

$$r1_a = r1 \oplus r1$$

$$r2 = -1$$

$$r3 = 234$$

$$r3_a = r2 \times r3$$

$$r4_a = r4 \oplus r4$$

$$r4_b = r4_a + r3_a$$

...

$$r3_d \neq 0$$

0014: ; ...

0020: ; ...

## A more complex example

```

0001: xor [r1, r1, r1_a]
0002: str [-1, , r2]
0003: str [234, , r3]
0004: mul [r2, r3, r3_a]
0005: xor [r4, r4, r4_a]
0006: add [r4_a, r3_a, r4_b]
0007: bsh [r4_b, 1, r5]
0008: add [in, r1_a, r1_b]
0009: sub [in, r3_a, in_a]
000a: bsh [in_a, 1, in_b]
000b: div [r5, 16, r4_c]
000c: mul [r3_a, 2, r3_b]
000d: add [in_b, r3_b, r3_c]
000e: mul [r3_c, r3_c, r5_a]
000f: add [r2, 5, r2_a]
0010: div [r5_a, r2_a, r5_b]
0011: add [r5_b, r1_b, r1_c]
0012: mod [r1_c, 2, r3_d]
0013: jcc [r3_d, , 0020]
  
```

### Take the conjunction

To reach 0014

$$r1_a = r1 \oplus r1$$

$$\wedge r2 = -1$$

$$\wedge r3 = 234$$

$$\wedge r3_a = r2 \times r3$$

$$\wedge r4_a = r4 \oplus r4$$

$$\wedge r4_b = r4_a + r3_a$$

...

$$\wedge r3_d = 0$$

0014: ; ...

0020: ; ...

## A more complex example

```

0001: xor [r1, r1, r1_a]
0002: str [-1, , r2]
0003: str [234, , r3]
0004: mul [r2, r3, r3_a]
0005: xor [r4, r4, r4_a]
0006: add [r4_a, r3_a, r4_b]
0007: bsh [r4_b, 1, r5]
0008: add [in, r1_a, r1_b]
0009: sub [in, r3_a, in_a]
000a: bsh [in_a, 1, in_b]
000b: div [r5, 16, r4_c]
000c: mul [r3_a, 2, r3_b]
000d: add [in_b, r3_b, r3_c]
000e: mul [r3_c, r3_c, r5_a]
000f: add [r2, 5, r2_a]
0010: div [r5_a, r2_a, r5_b]
0011: add [r5_b, r1_b, r1_c]
0012: mod [r1_c, 2, r3_d]
0013: jcc [r3_d, , 0020]
  
```

### Take the conjunction

To reach 0020

$$r1_a = r1 \oplus r1$$

$$\wedge r2 = -1$$

$$\wedge r3 = 234$$

$$\wedge r3_a = r2 \times r3$$

$$\wedge r4_a = r4 \oplus r4$$

$$\wedge r4_b = r4_a + r3_a$$

...

$$\wedge r3_d \neq 0$$

0014: ; ...

0020: ; ...



## A more complex example

```

0001: xor [r1, r1, r1_a]
0002: str [-1, , r2]
0003: str [234, , r3]
0004: mul [r2, r3, r3_a]
0005: xor [r4, r4, r4_a]
0006: add [r4_a, r3_a, r4_b]
0007: bsh [r4_b, 1, r5]
0008: add [in, r1_a, r1_b]
0009: sub [in, r3_a, in_a]
000a: bsh [in_a, 1, in_b]
000b: div [r5, 16, r4_c]
000c: mul [r3_a, 2, r3_b]
000d: add [in_b, r3_b, r3_c]
000e: mul [r3_c, r3_c, r5_a]
000f: add [r2, 5, r2_a]
0010: div [r5_a, r2_a, r5_b]
0011: add [r5_b, r1_b, r1_c]
0012: mod [r1_c, 2, r3_d]
0013: jcc [r3_d, , 0020]
  
```

**Check for satisfiability**

To reach 0014 ( $r3_d = 0$ )

$in = 0$

0014: ; ...

0020: ; ...

## A more complex example

```

0001: xor [r1, r1, r1_a]
0002: str [-1, , r2]
0003: str [234, , r3]
0004: mul [r2, r3, r3_a]
0005: xor [r4, r4, r4_a]
0006: add [r4_a, r3_a, r4_b]
0007: bsh [r4_b, 1, r5]
0008: add [in, r1_a, r1_b]
0009: sub [in, r3_a, in_a]
000a: bsh [in_a, 1, in_b]
000b: div [r5, 16, r4_c]
000c: mul [r3_a, 2, r3_b]
000d: add [in_b, r3_b, r3_c]
000e: mul [r3_c, r3_c, r5_a]
000f: add [r2, 5, r2_a]
0010: div [r5_a, r2_a, r5_b]
0011: add [r5_b, r1_b, r1_c]
0012: mod [r1_c, 2, r3_d]
0013: jcc [r3_d, , 0020]

```

### Check for satisfiability

To reach 0014 ( $r3_d = 0$ )

What other values for  $in = 0$  can reach 0014?

0014: ; ...

0020: ; ...

## A more complex example

```

0001: xor [r1, r1, r1_a]
0002: str [-1, , r2]
0003: str [234, , r3]
0004: mul [r2, r3, r3_a]
0005: xor [r4, r4, r4_a]
0006: add [r4_a, r3_a, r4_b]
0007: bsh [r4_b, 1, r5]
0008: add [in, r1_a, r1_b]
0009: sub [in, r3_a, in_a]
000a: bsh [in_a, 1, in_b]
000b: div [r5, 16, r4_c]
000c: mul [r3_a, 2, r3_b]
000d: add [in_b, r3_b, r3_c]
000e: mul [r3_c, r3_c, r5_a]
000f: add [r2, 5, r2_a]
0010: div [r5_a, r2_a, r5_b]
0011: add [r5_b, r1_b, r1_c]
0012: mod [r1_c, 2, r3_d]
0013: jcc [r3_d, , 0020]
  
```

### Check for satisfiability

To reach 0014 ( $r3_d = 0$ )

What other values for  $in$  can reach  
0014? Add additional constraint

Recheck for satisfiability

0014: ; ...

0020: ; ...

## A more complex example

```

0001: xor [r1, r1, r1_a]
0002: str [-1, , r2]
0003: str [234, , r3]
0004: mul [r2, r3, r3_a]
0005: xor [r4, r4, r4_a]
0006: add [r4_a, r3_a, r4_b]
0007: bsh [r4_b, 1, r5]
0008: add [in, r1_a, r1_b]
0009: sub [in, r3_a, in_a]
000a: bsh [in_a, 1, in_b]
000b: div [r5, 16, r4_c]
000c: mul [r3_a, 2, r3_b]
000d: add [in_b, r3_b, r3_c]
000e: mul [r3_c, r3_c, r5_a]
000f: add [r2, 5, r2_a]
0010: div [r5_a, r2_a, r5_b]
0011: add [r5_b, r1_b, r1_c]
0012: mod [r1_c, 2, r3_d]
0013: jcc [r3_d, , 0020]
  
```

**Check for satisfiability**

To reach 0020 ( $r3_d \neq 0$ )

0014: ; ...

0020: ; ...

## A more complex example

```

0001: xor [r1, r1, r1_a]
0002: str [-1, , r2]
0003: str [234, , r3]
0004: mul [r2, r3, r3_a]
0005: xor [r4, r4, r4_a]
0006: add [r4_a, r3_a, r4_b]
0007: bsh [r4_b, 1, r5]
0008: add [in, r1_a, r1_b]
0009: sub [in, r3_a, in_a]
000a: bsh [in_a, 1, in_b]
000b: div [r5, 16, r4_c]
000c: mul [r3_a, 2, r3_b]
000d: add [in_b, r3_b, r3_c]
000e: mul [r3_c, r3_c, r5_a]
000f: add [r2, 5, r2_a]
0010: div [r5_a, r2_a, r5_b]
0011: add [r5_b, r1_b, r1_c]
0012: mod [r1_c, 2, r3_d]
0013: jcc [r3_d, , 0020]
  
```

**Check for satisfiability**

To reach 0020 ( $r3_d \neq 0$ )

Unsatisfiable

0014: ; ...

0020: ; ...

## A more complex example

```

0001: xor [r1, r1, r1_a]
0002: str [-1, , r2]
0003: str [234, , r3]
0004: mul [r2, r3, r3_a]
0005: xor [r4, r4, r4_a]
0006: add [r4_a, r3_a, r4_b]
0007: bsh [r4_b, 1, r5]
0008: add [in, r1_a, r1_b]
0009: sub [in, r3_a, in_a]
000a: bsh [in_a, 1, in_b]
000b: div [r5, 16, r4_c]
000c: mul [r3_a, 2, r3_b]
000d: add [in_b, r3_b, r3_c]
000e: mul [r3_c, r3_c, r5_a]
000f: add [r2, 5, r2_a]
0010: div [r5_a, r2_a, r5_b]
0011: add [r5_b, r1_b, r1_c]
0012: mod [r1_c, 2, r3_d]
0013: jcc [r3_d, , 0020]
  
```

**Check for satisfiability**

To reach 0020 ( $r3_d \neq 0$ )

Unsatisfiable

This is an **opaque predicate** – no need to RE this path

0014: ; ...

0020: ; ...

## Summary

- Applications
  - Opaque predicate detection
  - Dead-code detection
  - Automatic exploit generation (AEG)
- Loops?
  - Typically unrolled

## Summary

- Applications
  - Opaque predicate detection
  - Dead-code detection
  - Automatic exploit generation (AEG)
- Loops?
  - Typically unrolled

## Challenges

- SMT solvers may not be able to solve complex formulas
- Unbounded/infinite loops
- Appropriate semantics



# Symbolic execution

## Introduction

### Previously

Statically modelled code as first-order logic formulas

## Introduction

### Previously

Statically modelled code as first-order logic formulas

### Now

Run program through interpreter that operates on **symbolic** values and generate logic formulas dynamically

## Open-source tools

**TRILON**

Dynamic Binary Analysis

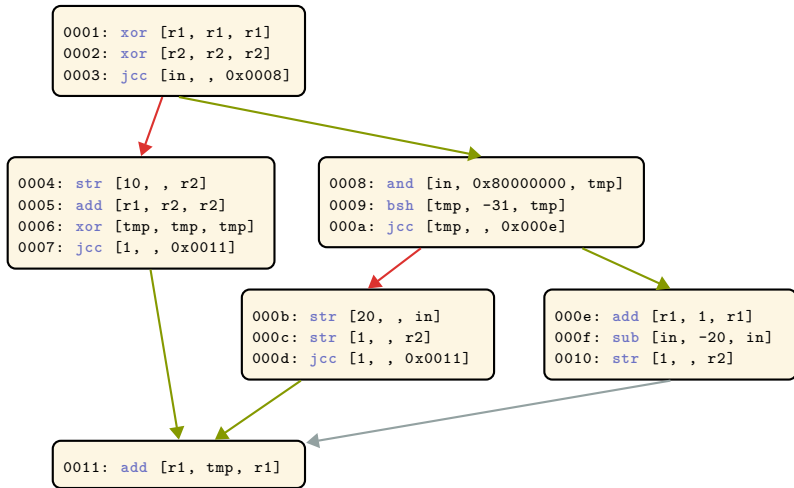


**S2E**

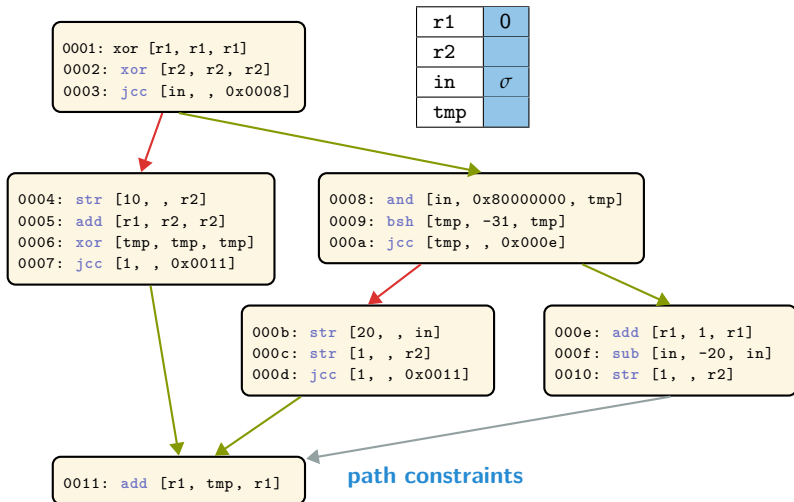
## General approach

- Program input is provided as **symbolic** values (rather than **concrete**)
- Operations (e.g. addition, assignment, etc.) operate on these symbolic values to generate **symbolic expressions**
- Conditional statements (e.g. `jcc`) result in a **fork** – both paths are explored
- Invoke an SMT solver to find a solution to the symbolic expressions – this is a concrete input for the path explored

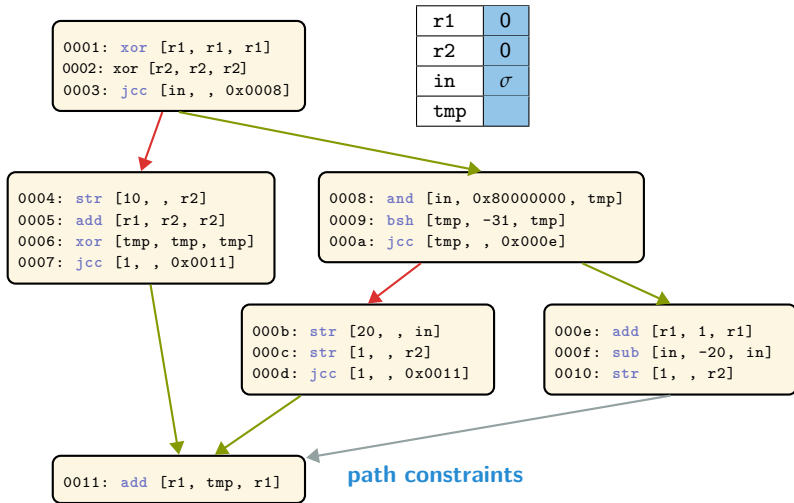
## Example



## Example

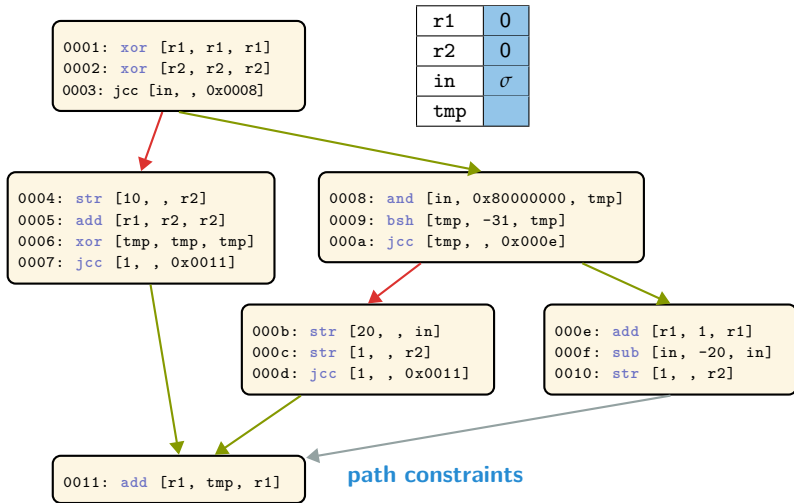


## Example

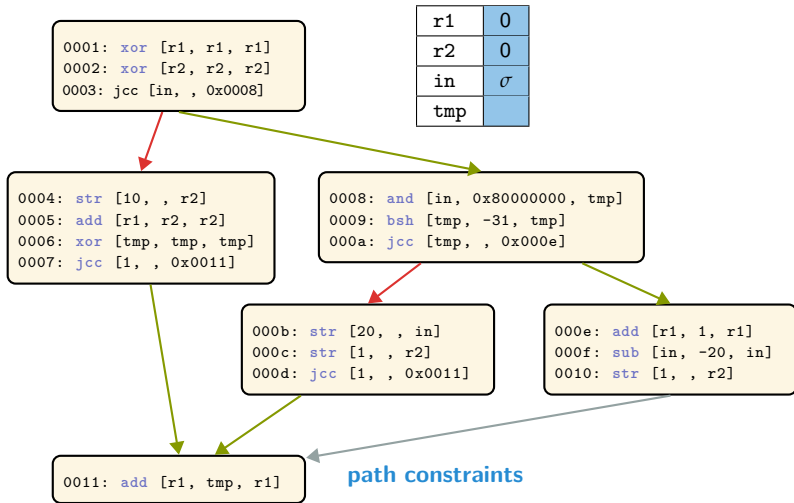




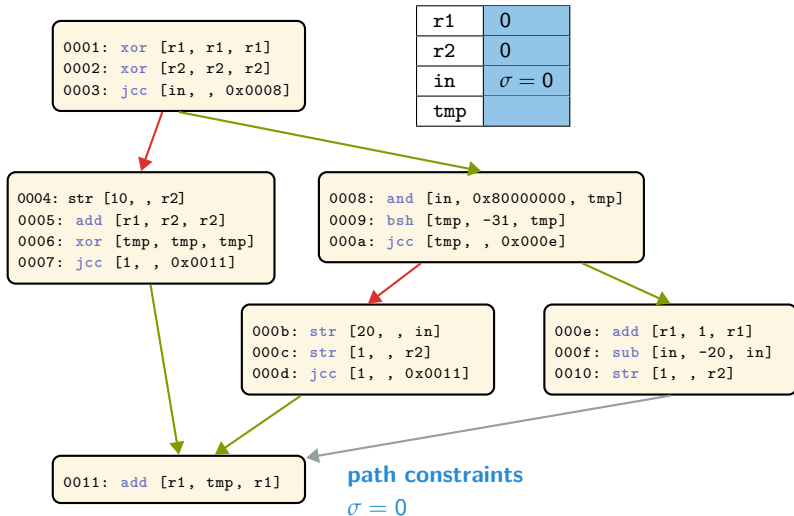
## Example



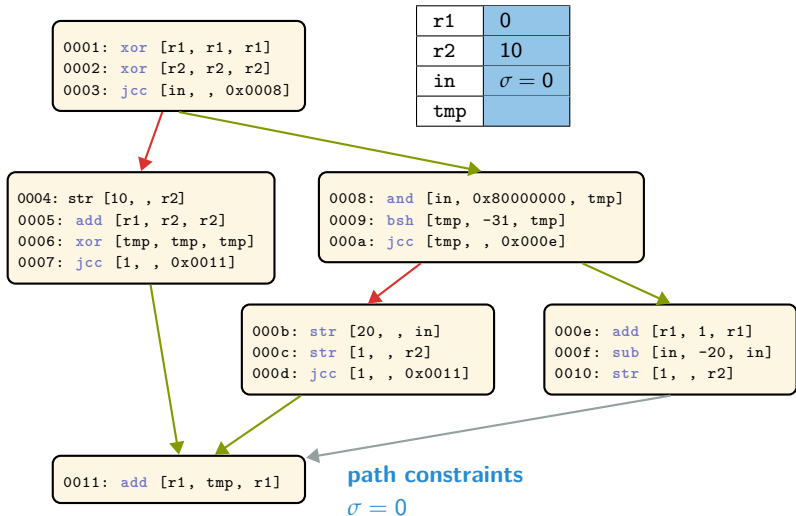
## Example



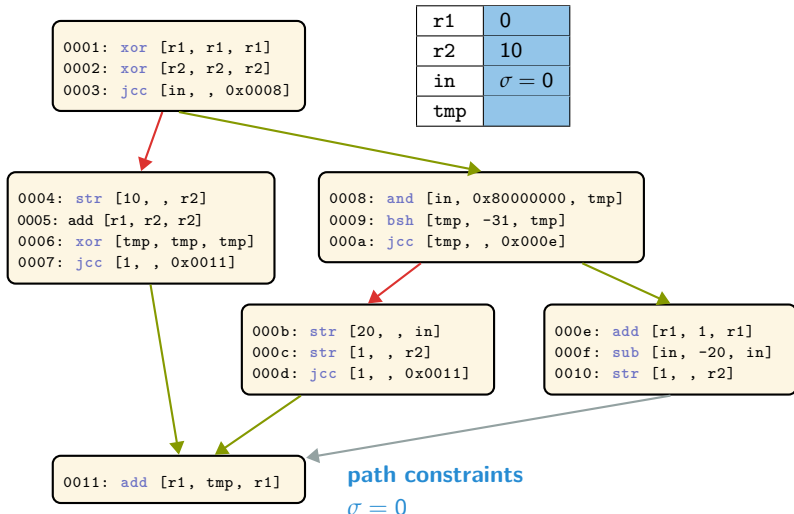
## Example



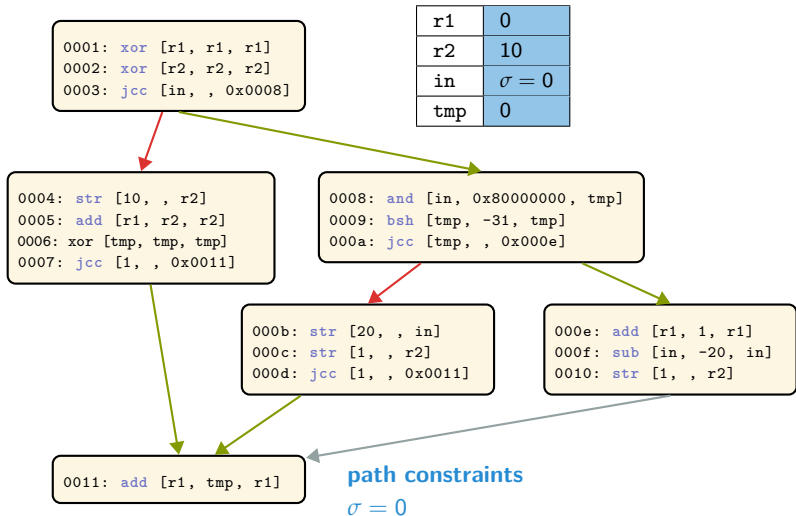
## Example



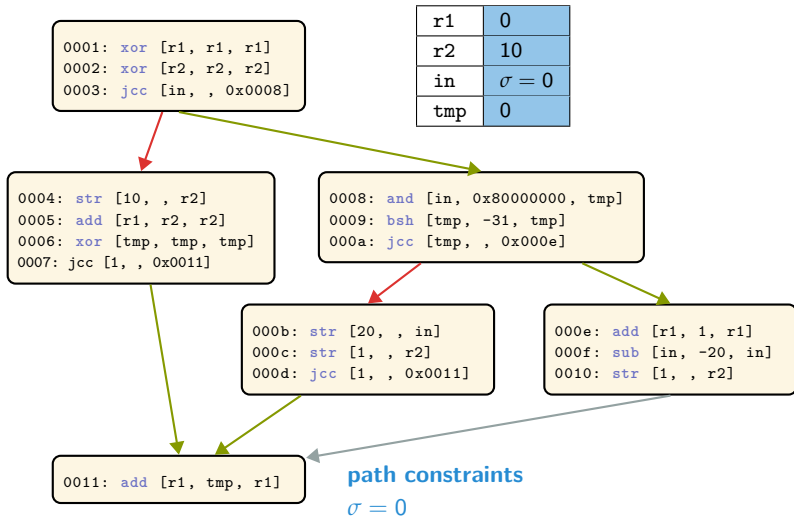
## Example



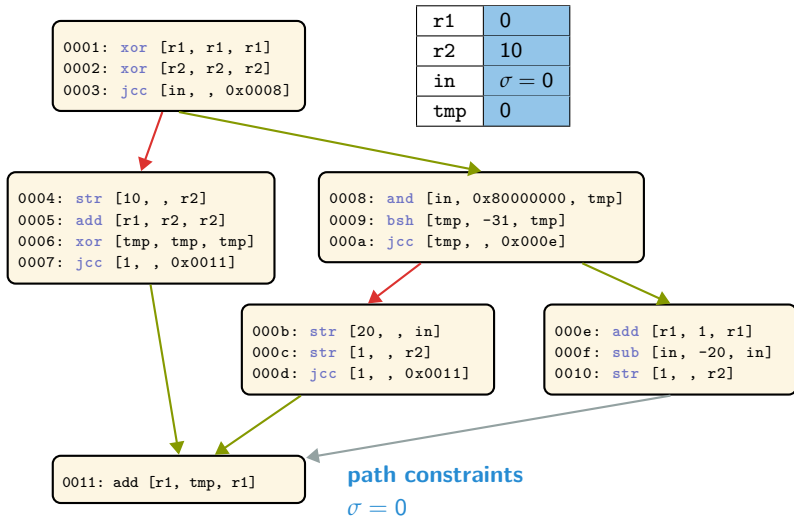
## Example



## Example

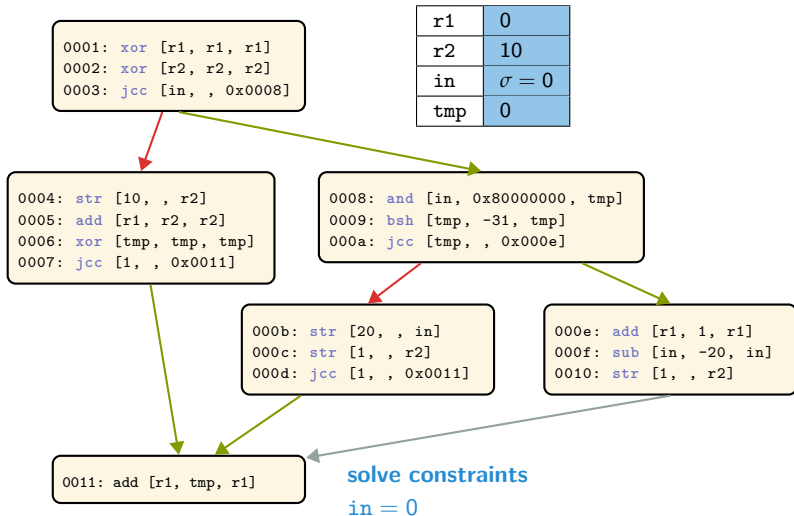


## Example

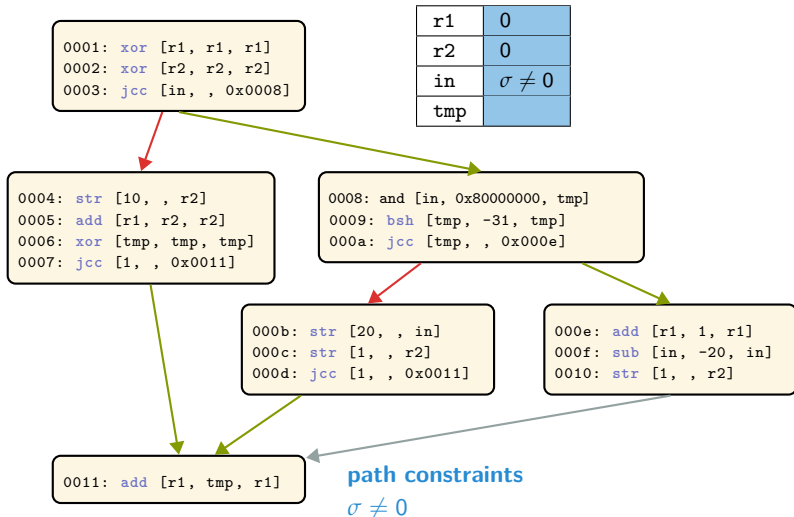




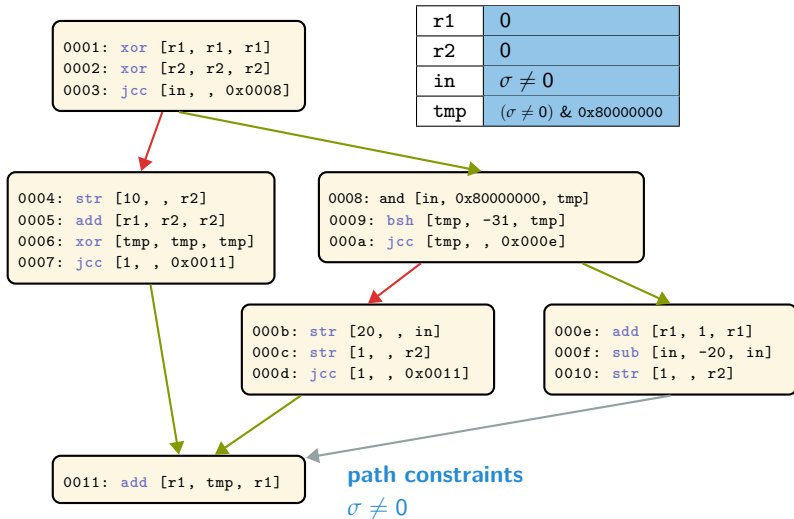
## Example



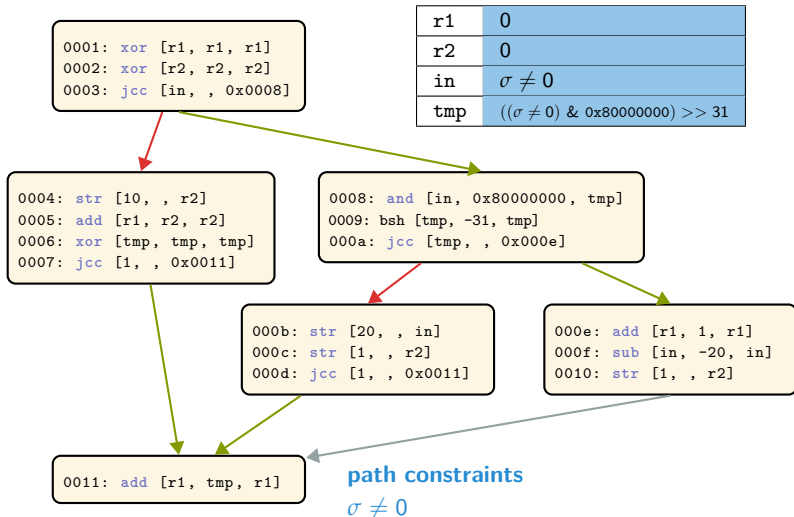
## Example



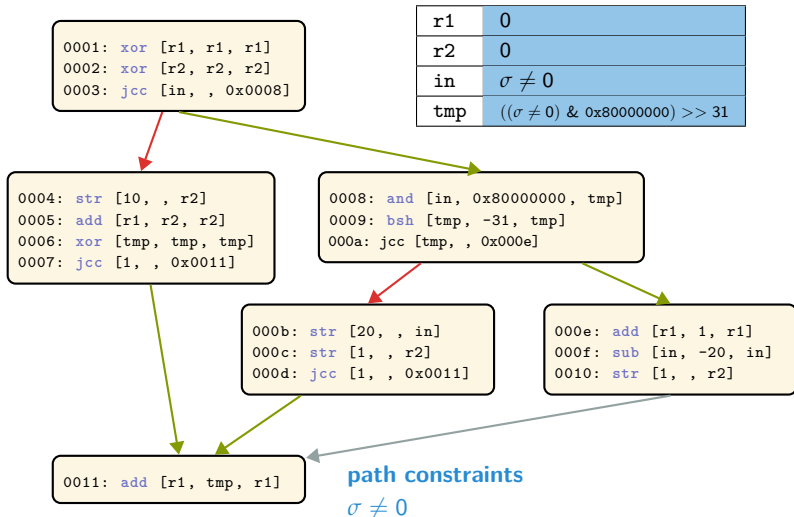
## Example



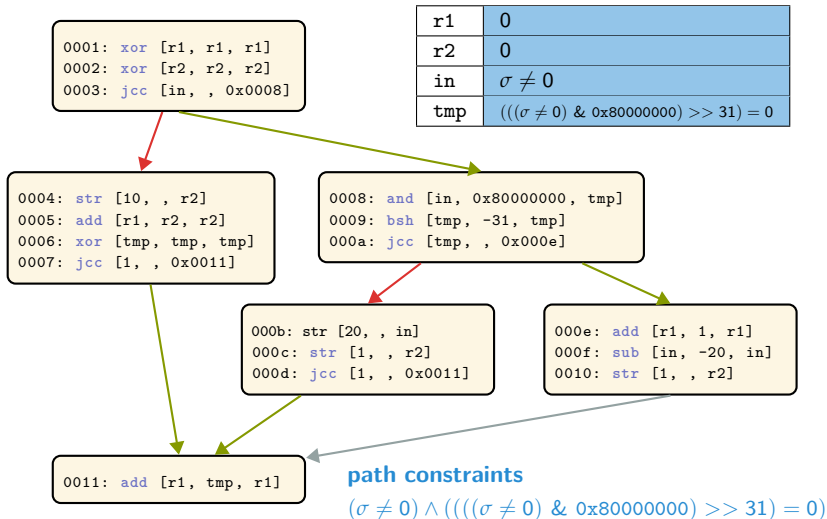
## Example



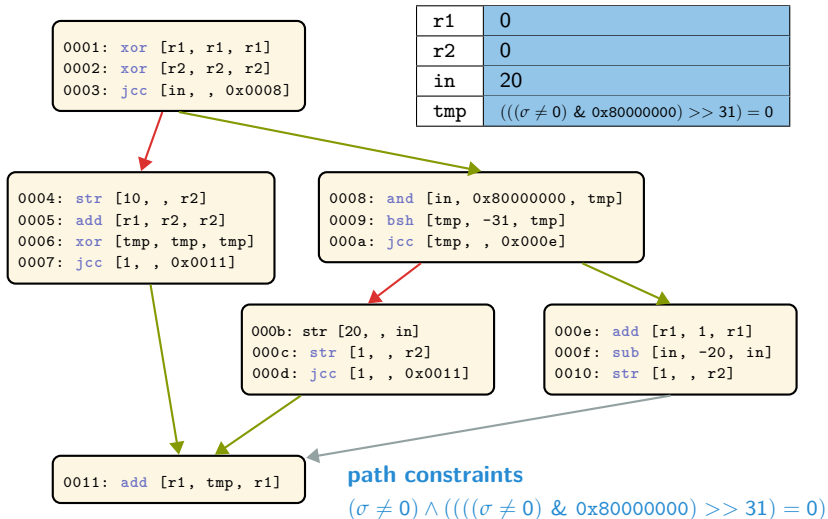
## Example



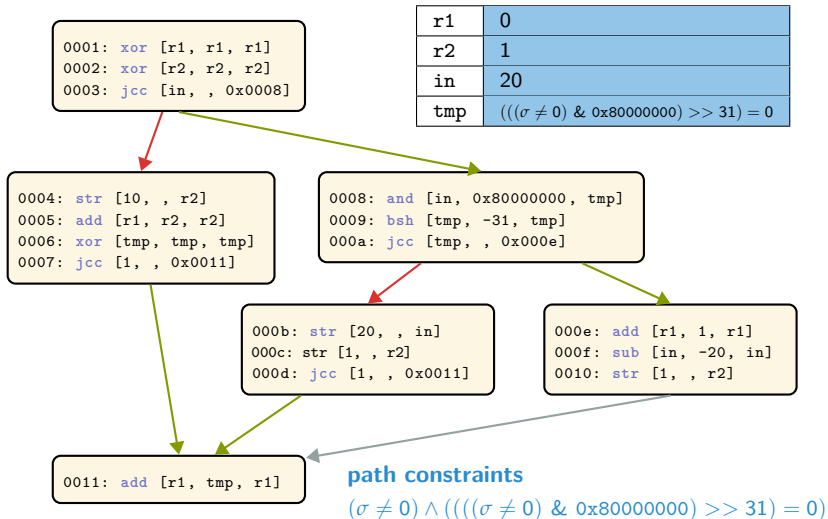
## Example



## Example

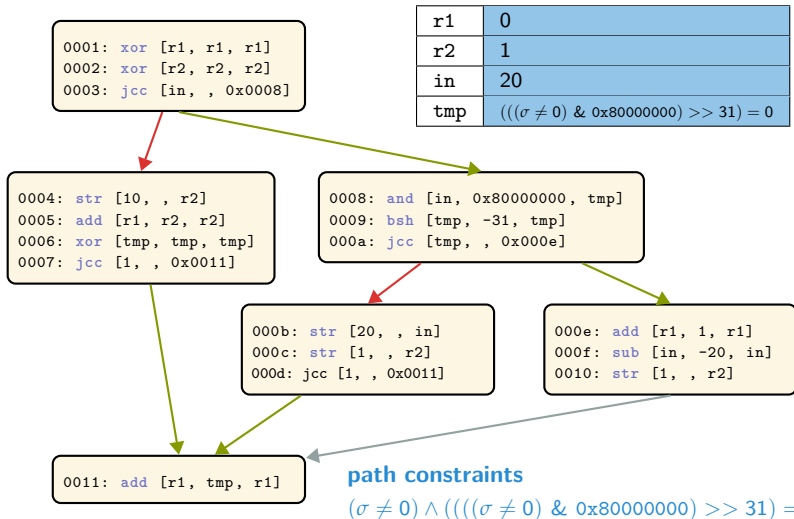


## Example

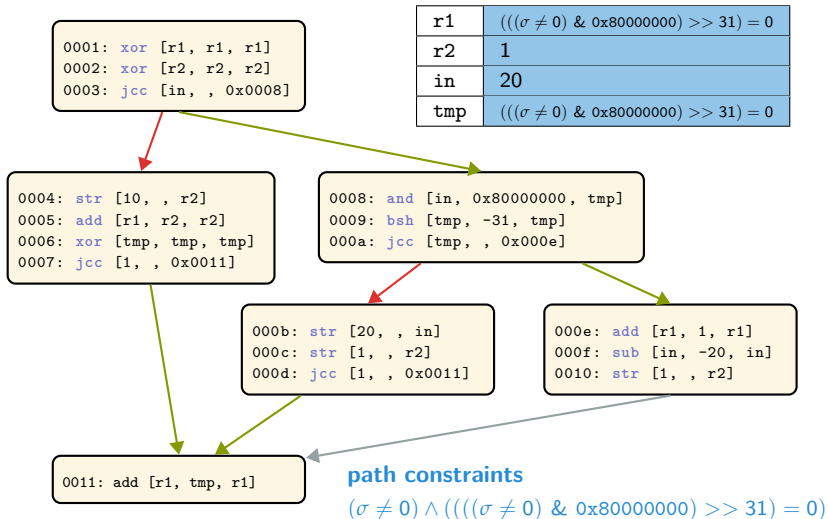




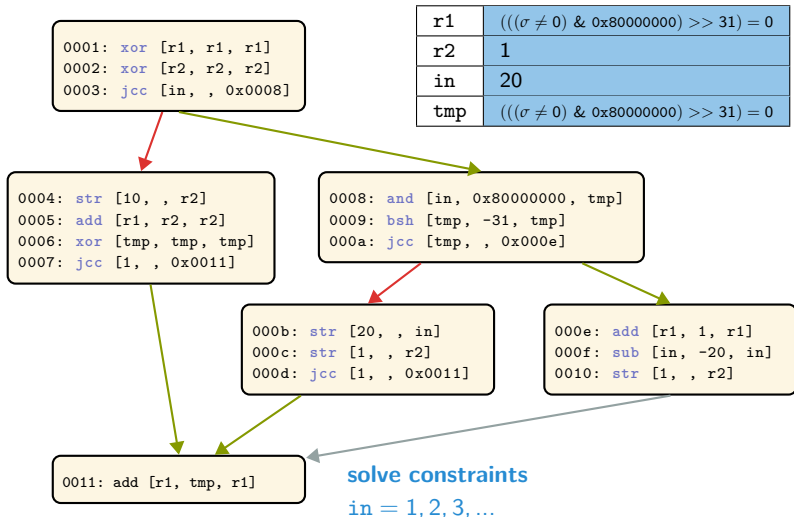
## Example



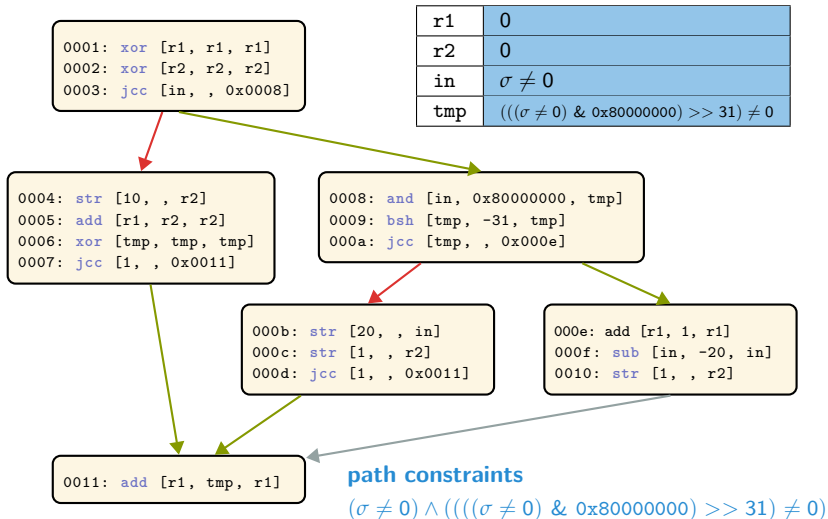
## Example



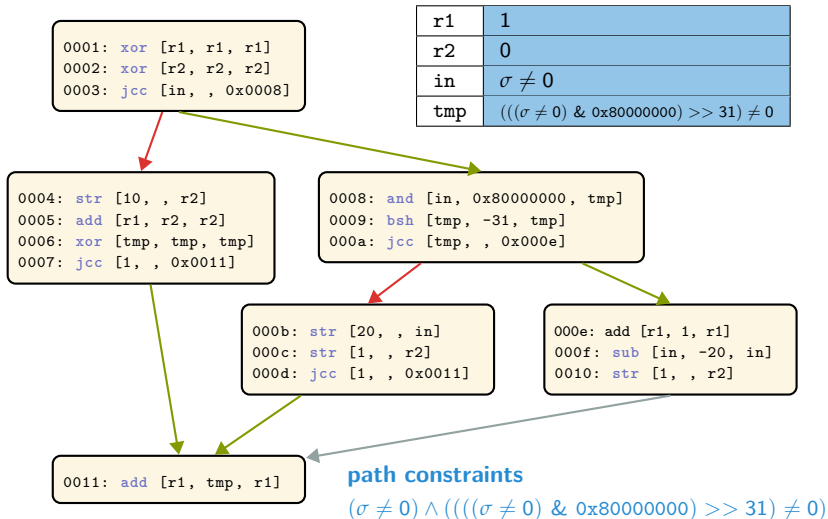
## Example



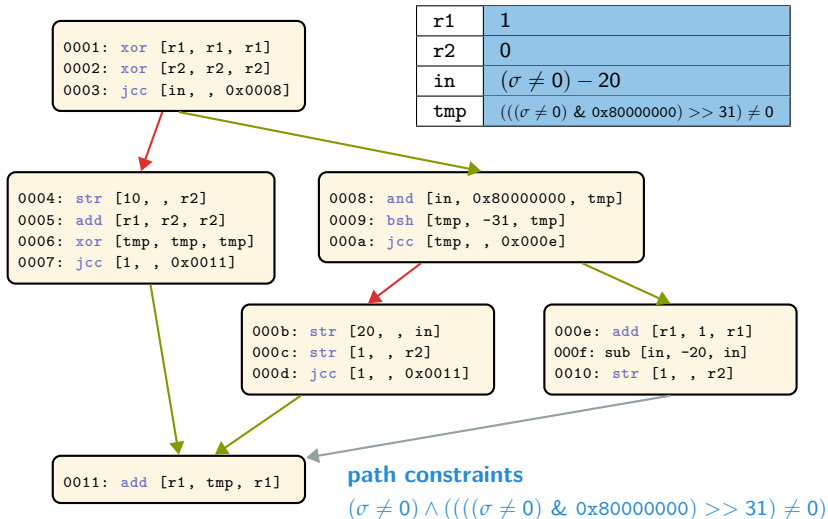
## Example



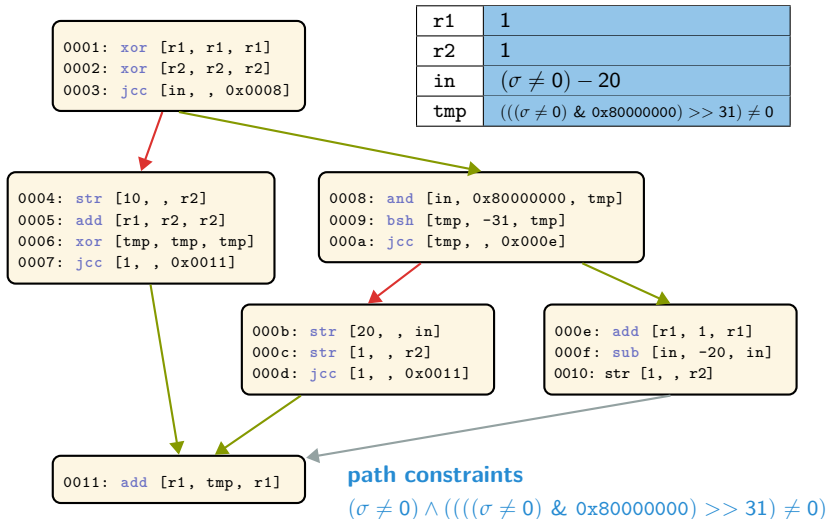
## Example



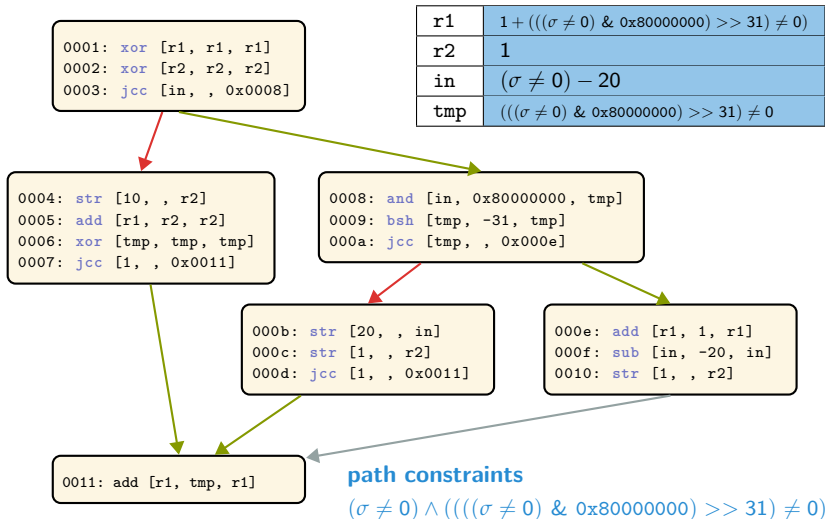
## Example



## Example

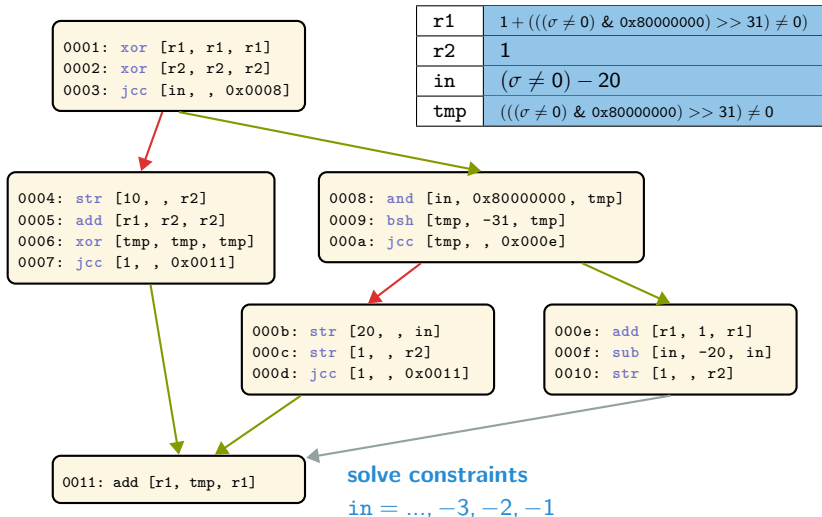


## Example





## Example



## Summary

- Applications
  - Automatic test-case generation
  - Vulnerability discovery (with fuzzing)
  - Malware analysis (explore “trigger sources”)
- Loops?
  - Quickly result in **state-space explosion**
  - Possibly **model** common library functions
    - E.g. strlen, strcpy, memcpy, etc.

## Summary

- Applications
  - Automatic test-case generation
  - Vulnerability discovery (with fuzzing)
  - Malware analysis (explore “trigger sources”)
- Loops?
  - Quickly result in **state-space explosion**
  - Possibly **model** common library functions
    - E.g. strlen, strcpy, memcpy, etc.

## Challenges

- State-space explosion
- Path (state) selection/prioritisation
- Environment modelling

# Abstract interpretation

## Why abstract interpretation?

### Rice's Theorem

Any *non-trivial* property of program behaviour is undecidable

## Why abstract interpretation?

### Rice's Theorem

Any *non-trivial* property of program behaviour is undecidable

### Solution?

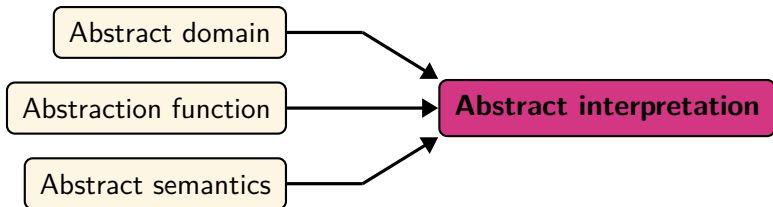


## What is abstract interpretation?

**Abstract** the semantics of our program to make analysis possible

## What is abstract interpretation?

**Abstract** the semantics of our program to make analysis possible





## Abstract domain

Instead of operating on an (infinitely large) set of concrete values, operate on a smaller set of values that **approximates** the concrete values.

## Abstract domain

Instead of operating on an (infinitely large) set of concrete values, operate on a smaller set of values that **approximates** the concrete values.

Domain	Values
Sign	$-, 0, +$
Interval	$[l, u]$ , where $l$ and $u$ are integers and $l \leq u$

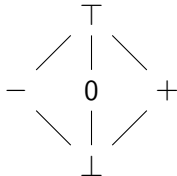
## Abstract domain

Abstract values must form a lattice. The lattice is used when states are **joined** (merged) during execution.

## Abstract domain

Abstract values must form a lattice. The lattice is used when states are **joined** (merged) during execution.

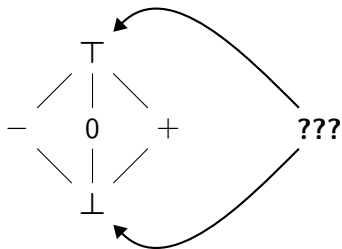
### Sign domain



## Abstract domain

Abstract values must form a lattice. The lattice is used when states are **joined** (merged) during execution.

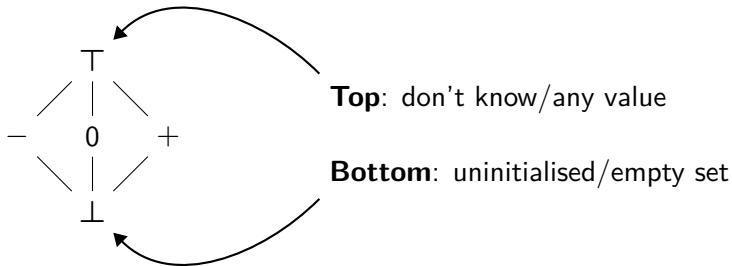
### Sign domain



## Abstract domain

Abstract values must form a lattice. The lattice is used when states are **joined** (merged) during execution.

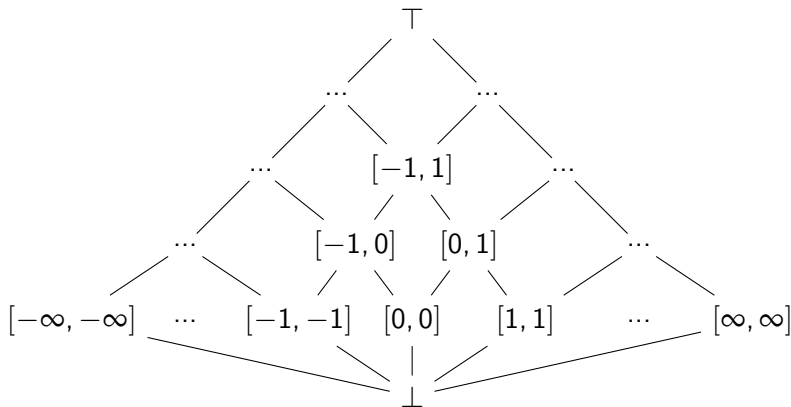
### Sign domain



## Abstract domain

Abstract values must form a lattice. The lattice is used when states are **merged** during execution.

### Interval domain



## Abstraction function

Go from concrete  $\rightarrow$  abstract



## Abstraction function

Go from concrete  $\rightarrow$  abstract

### Sign domain

Concrete	Abstract
{}	$\perp$

## Abstraction function

Go from concrete  $\rightarrow$  abstract

### Sign domain

Concrete	Abstract
$\{\}$	$\perp$
$\{10\}$	$+$

## Abstraction function

Go from concrete  $\rightarrow$  abstract

### Sign domain

Concrete	Abstract
$\{\}$	$\perp$
$\{10\}$	$+$
$\{10, 5\}$	$+$

## Abstraction function

Go from concrete  $\rightarrow$  abstract

### Sign domain

Concrete	Abstract
$\{\}$	$\perp$
$\{10\}$	$+$
$\{10, 5\}$	$+$
$\{-10, -5, -33\}$	$-$

## Abstraction function

Go from concrete  $\rightarrow$  abstract

### Sign domain

Concrete	Abstract
$\{\}$	$\perp$
$\{10\}$	$+$
$\{10, 5\}$	$+$
$\{-10, -5, -33\}$	$-$
$\{10, 1, -5\}$	$\top$

## Abstraction function

Go from concrete  $\rightarrow$  abstract

### Interval domain

Concrete	Abstract
{}	$\perp$

## Abstraction function

Go from concrete  $\rightarrow$  abstract

### Interval domain

Concrete	Abstract
$\{\}$	$\perp$
$\{10\}$	$[10, 10]$

## Abstraction function

Go from concrete  $\rightarrow$  abstract

### Interval domain

Concrete	Abstract
$\{\}$	$\perp$
$\{10\}$	$[10, 10]$
$\{10, 5\}$	$[5, 10]$



## Abstraction function

Go from concrete  $\rightarrow$  abstract

### Interval domain

Concrete	Abstract
$\{\}$	$\perp$
$\{10\}$	$[10, 10]$
$\{10, 5\}$	$[5, 10]$
$\{-10, -5, -33\}$	$[-33, -5]$

## Abstraction function

Go from concrete  $\rightarrow$  abstract

### Interval domain

Concrete	Abstract
$\{\}$	$\perp$
$\{10\}$	$[10, 10]$
$\{10, 5\}$	$[5, 10]$
$\{-10, -5, -33\}$	$[-33, -5]$
$\{10, 1, -5\}$	$[-5, 10]$

## Abstract semantics

Give **meaning** to our program in the abstract domain

## Abstract semantics

Give **meaning** to our program in the abstract domain

**Sign domain**

`add [DWORD r1, DWORD r2, DWORD r3]`

			r2		
			-	0	+
			-	-	T
r1	0	-	0	+	+
	+	T	+	+	+

## Abstract semantics

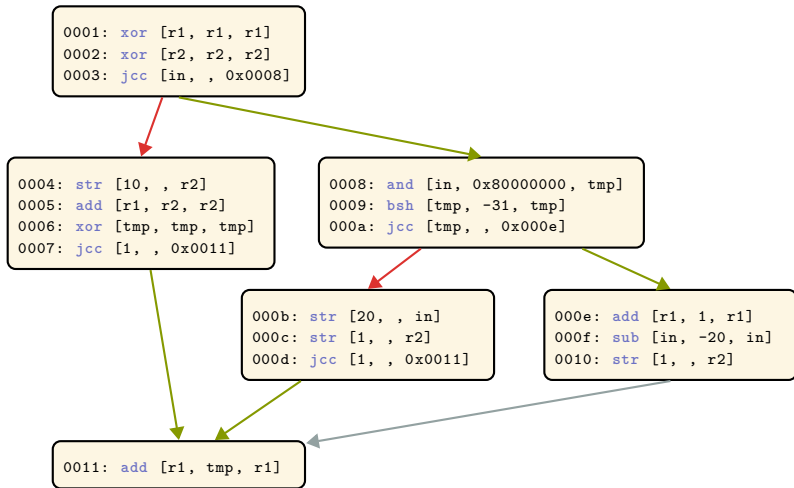
Give **meaning** to our program in the abstract domain

**Interval domain**

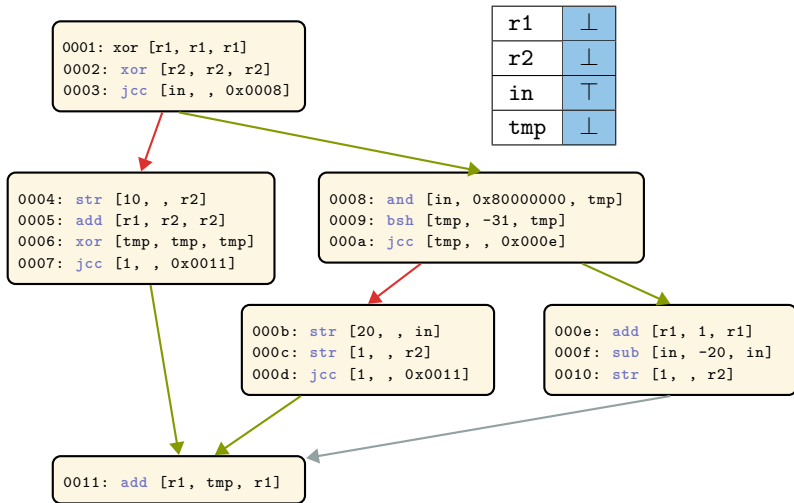
`add [DWORD r1, DWORD r2, DWORD r3]`

$$\begin{array}{c}
 r2 \\
 [x, y] \\
 \hline
 r1 \quad [a, b] \quad | \quad [a + x, b + y]
 \end{array}$$

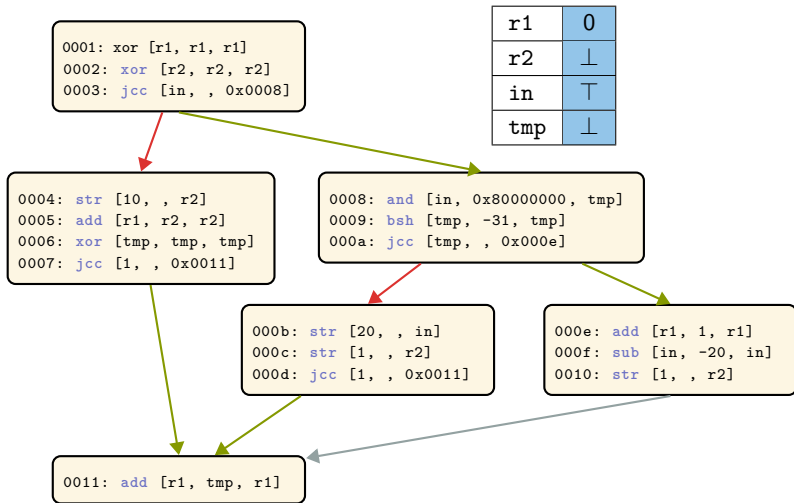
## Example – sign analysis



## Example – sign analysis

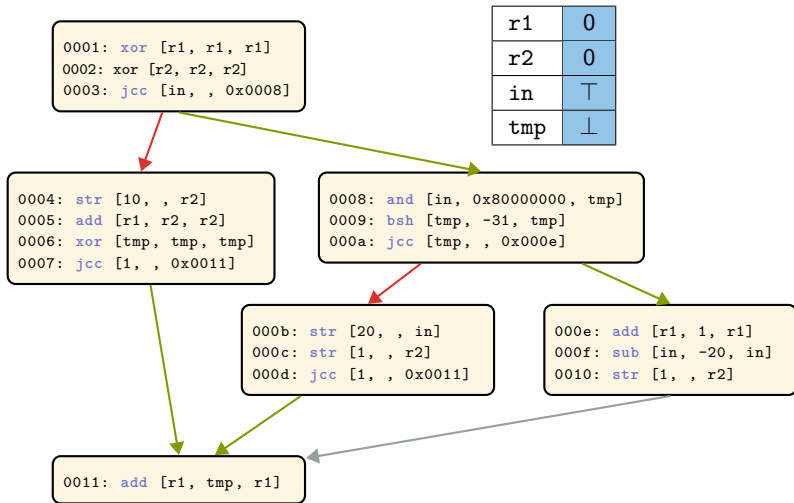


## Example – sign analysis

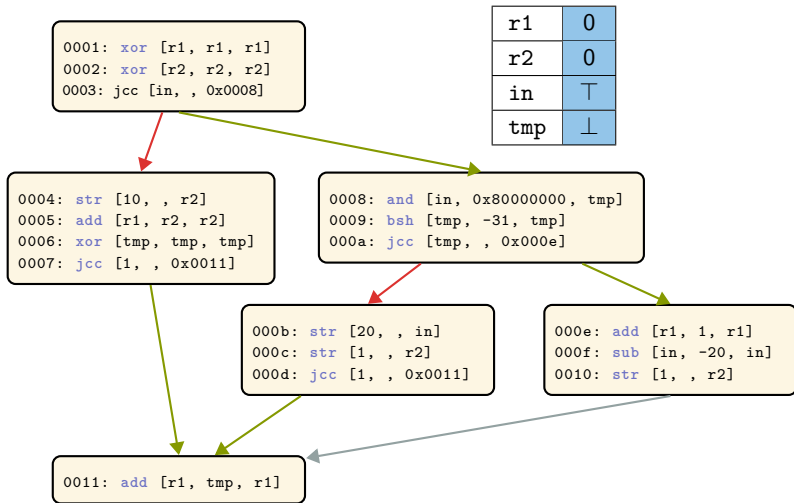




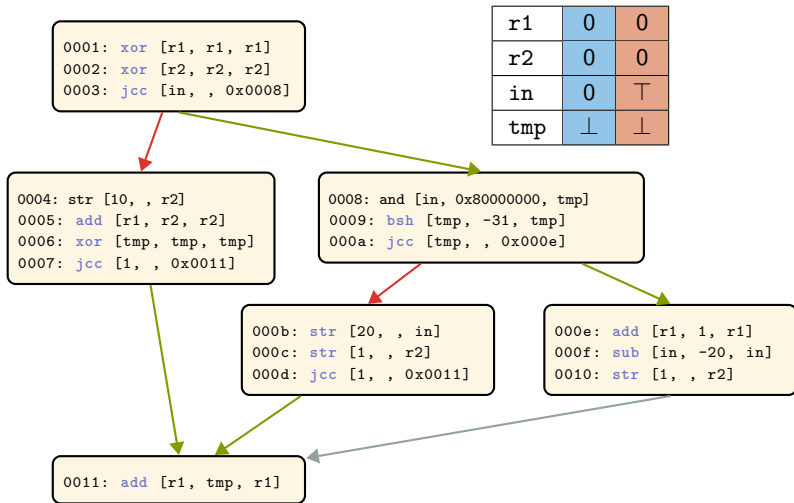
## Example – sign analysis



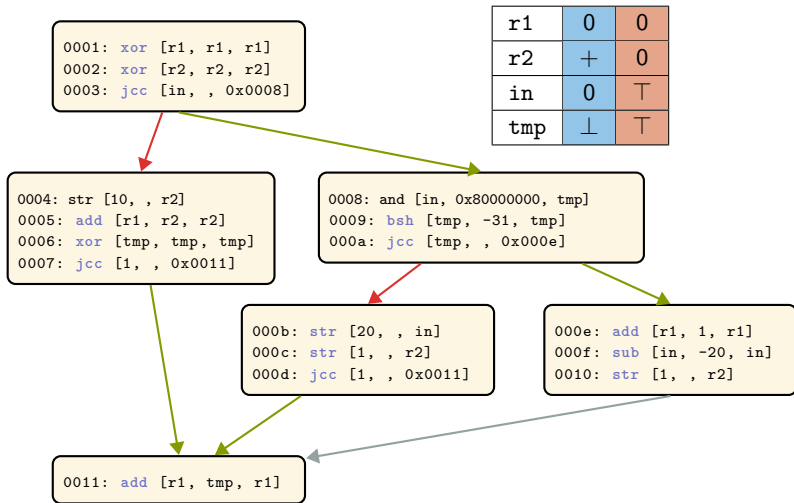
## Example – sign analysis



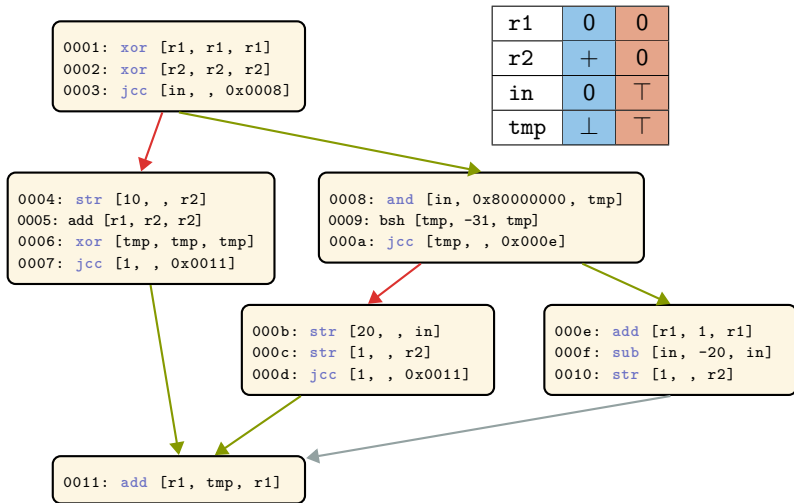
## Example – sign analysis



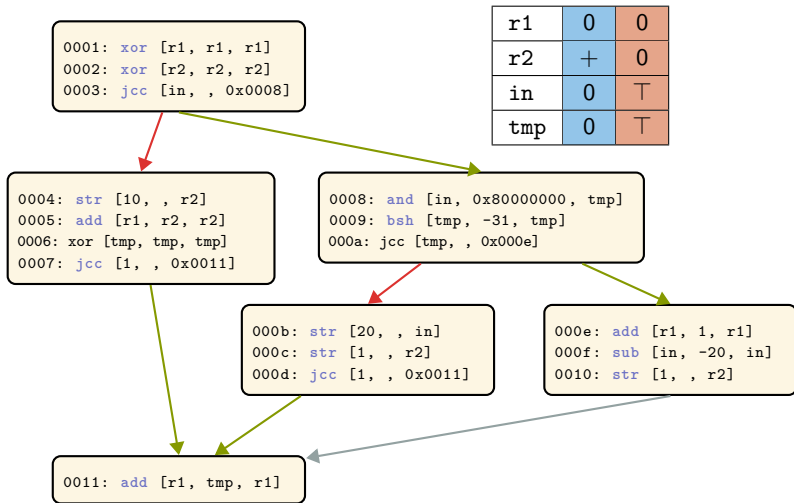
## Example – sign analysis



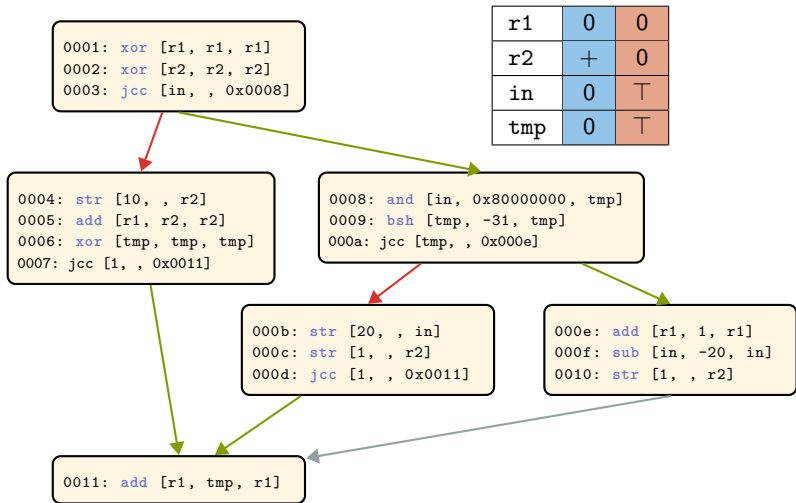
## Example – sign analysis



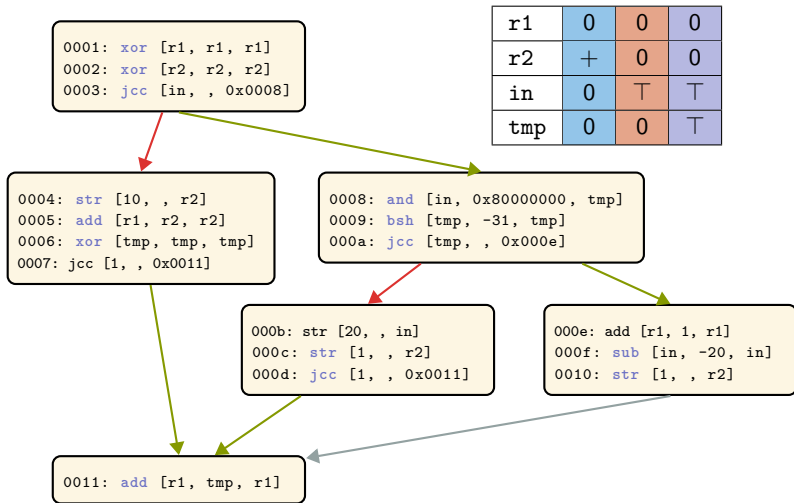
## Example – sign analysis



## Example – sign analysis

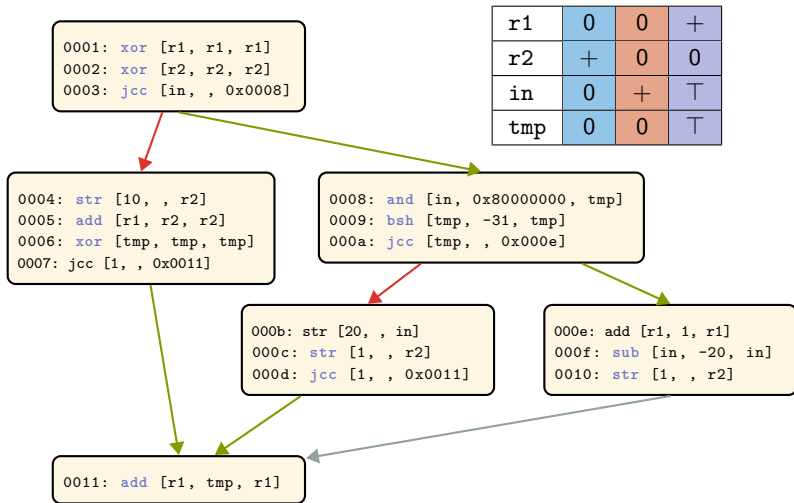


## Example – sign analysis

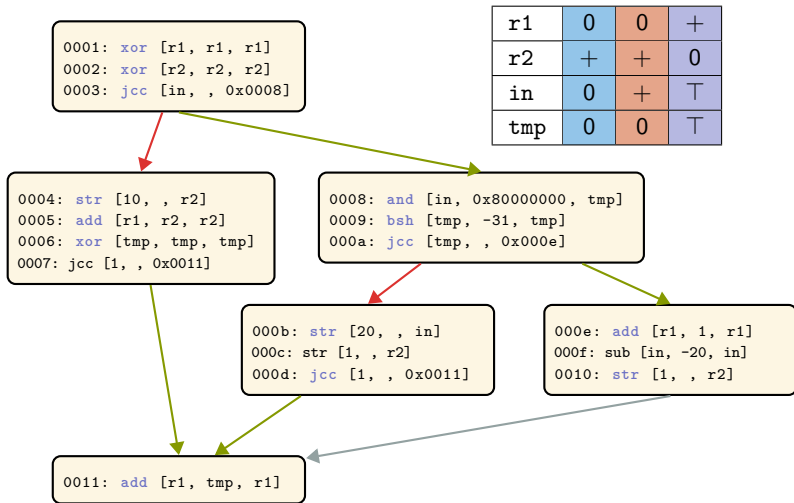




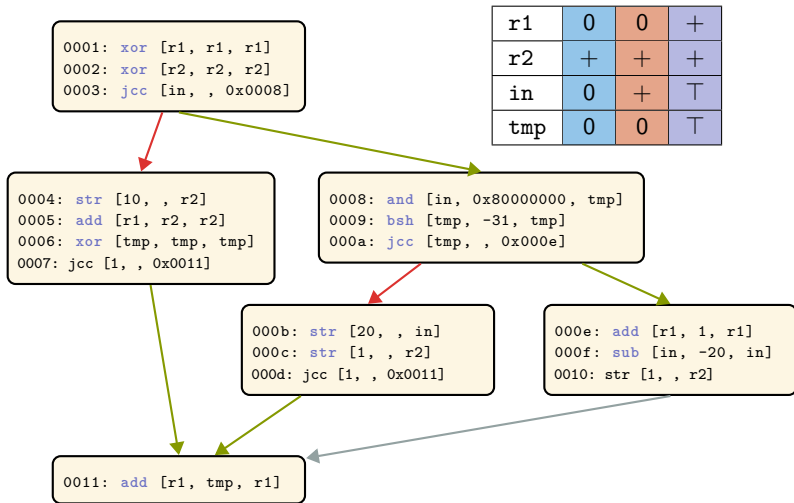
## Example – sign analysis



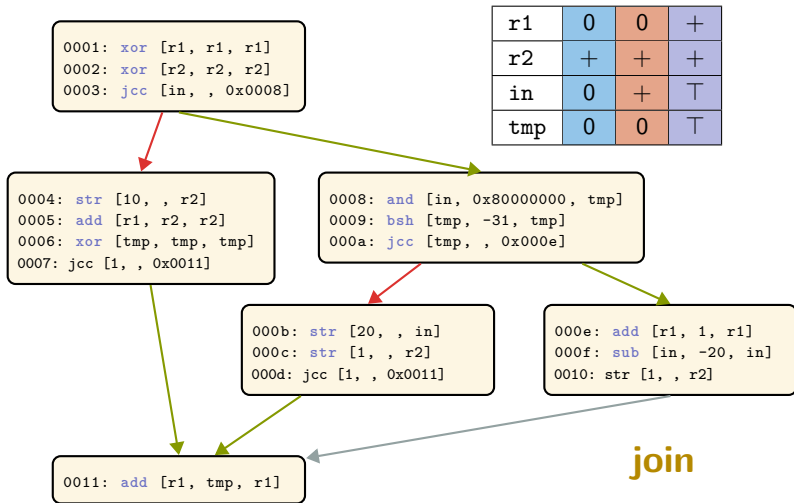
## Example – sign analysis



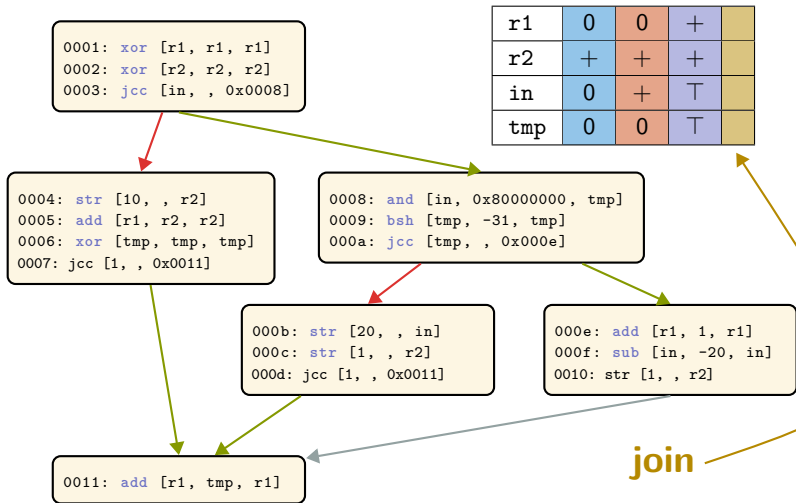
## Example – sign analysis



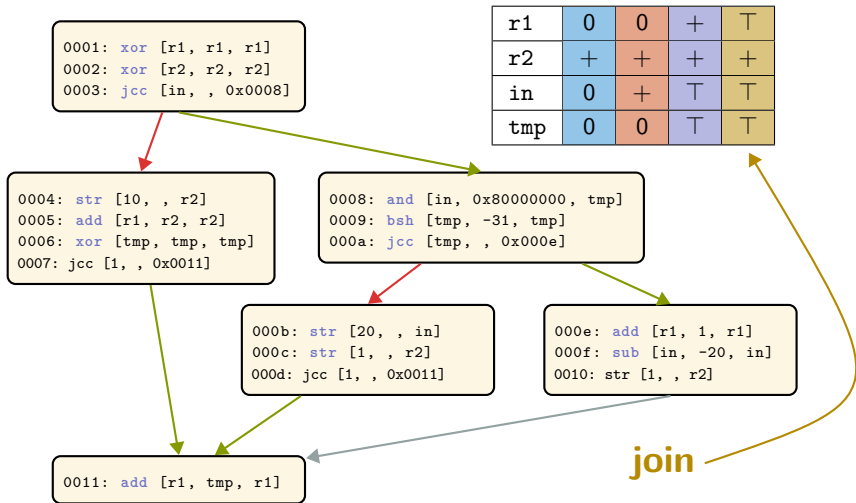
## Example – sign analysis



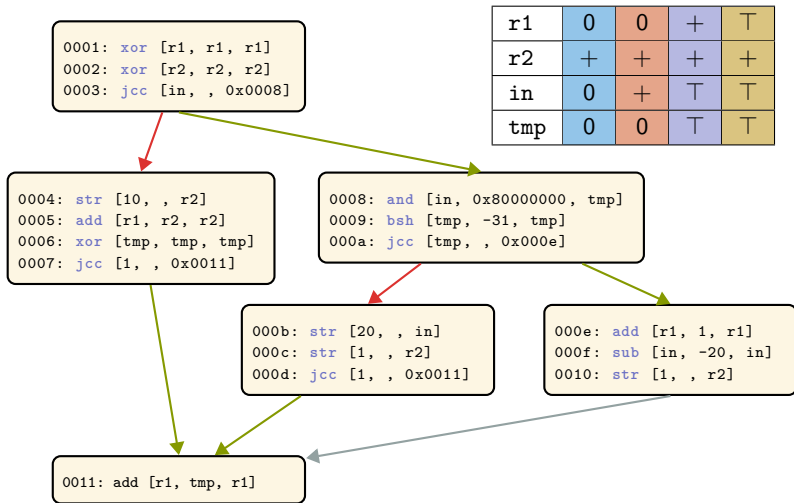
## Example – sign analysis



## Example – sign analysis



## Example – sign analysis



## Summary

- Abstract interpretation is hard on binary code
  - Could we have done better with a more complex abstract domain (e.g. intervals)?
- Accuracy vs. cost
- Loops?
  - Employ **widening** operator



## Summary

- Abstract interpretation is hard on binary code
  - Could we have done better with a more complex abstract domain (e.g. intervals)?
- Accuracy vs. cost
- Loops?
  - Employ **widening** operator

## Challenges

- How do we design a suitable abstract domain?
- How do we accurately represent the semantics of our instruction set?

# Conclusion

## Summary

- Given you a taste of what techniques exist

## Summary

- Given you a taste of what techniques exist
- Binary program analysis is undergoing a renaissance

## Summary

- Given you a taste of what techniques exist
- Binary program analysis is undergoing a renaissance
  - Thanks to DARPA Cyber Grand Challenge

## Summary

- Given you a taste of what techniques exist
- Binary program analysis is undergoing a renaissance
  - Thanks to DARPA Cyber Grand Challenge
- Still a lot of work to go

## Summary

- Given you a taste of what techniques exist
- Binary program analysis is undergoing a renaissance
  - Thanks to DARPA Cyber Grand Challenge
- Still a lot of work to go
  - How do we deal with state-space explosion?

## Summary

- Given you a taste of what techniques exist
- Binary program analysis is undergoing a renaissance
  - Thanks to DARPA Cyber Grand Challenge
- Still a lot of work to go
  - How do we deal with state-space explosion?
  - How do we scale these techniques?



## Summary

- Given you a taste of what techniques exist
- Binary program analysis is undergoing a renaissance
  - Thanks to DARPA Cyber Grand Challenge
- Still a lot of work to go
  - How do we deal with state-space explosion?
  - How do we scale these techniques?
  - Not many open-source tools (symbolic execution is the exception)



# Thank you!